

# **ENGG4102**

<i a Ub]hUf]Ub 9b[]bYYf]b[ Dfc YWh</pre>



# 7ci fgY<sup>\*</sup>Cj Yfj ]Yk

## GHJZZ:7cbHJWh:8YHJ]`g

## 7cbj Ybcfg

BUa Y	9a U]`	5j U]`UV]`] <b>m</b>	@cWUh]cb	D\cbY
5bXfYk *8Ubg]Y	U"XUbg]Y4 i bgk "YXi "Ui	D`YUgY`UffUb[Y h]a Y`hc`a YYh	< &\$ F cca ' \$*	Ž*%'&'-',) *%+*

G\\cc`7cbHJ\\n±2cfaUh]cb

‰

‰

9b[]bYYf<mark>9tt[:16tY%Njbh[:1GihdXY6thiGYfjdVXfgGYf9bV[/b</mark>YYff]bY;16thVXXYbdy:1GYdttcfthYdXffjdVWfgfYgg]cb:VXYV<u>g</u>žW

YdfBi WYi g

## 7ci fgY 8YW] g

I b]hg cZ7fYX]h\*

#### Gi a a UfmcZh\Y 7ci fgY

DfcYWg'Wci `X']bWi XY'Ubmcf'U```cZh\Y'Zc``ck]b['WcadcbYbhg'Ug'Uddfcdf]UhY'hc'h\Y']XYbh]Z]YX'dfcV'Ya.

- VUW\_[fcibXfYj]Yk cZbYYXgžWcbH/lh
- XYj Y`cda YbhcZdchYbhJU``gc`i hJcbgž']bWl X]b[ 'fYj ]Yk 'cZYl ]ghJb[ 'XUhUž'fYgYUfWk 'UbX'hYWkbc`c[ ]Yg Ug'Uddfcdf]UhY

@YUfb]b[ 'Ci HWca Y	95 GHJ[Y %7ca dYHYbW]Yg
%":7f]h]WU``mUbU`mgY'Yb[]bYYf]b['dfcV`Yag']b'bYk'UbX'W\U``Yb[]b[ WcbhYl hg'UbX'XYj Y`cd'WfYUh]j Y'gc`i h]cbg'Udd`m]b['Yb[]bYYf]b[ X]gW]d`]bY'_bck`YX[Y"	D9%" ž'D9%"(ž'D9%")
&"`5dd`mUddfcdf]UhY`hYW\bc`c[mUbX`Yb[]bYYf]b[`gmghYa`XYg][bdf]bW]d`Yg`hc`\i a Ub]hUf]Ub`Yb[]bYYf]b[`WcbhYl hg`]bWcfdcfUh]b[gcW]U`žYWcbca]WUbX`Ybj]fcbaYbhU``ZUWcfg	D9%"*žD9&"&
' "'5dd`mgmghYa Uh]WYb[]bYYf]b['UddfcUWXYg'hc'hXY'a UbU[Ya YbhcZUb'Yb[]bYYf]b['dfc'YWn'	D9&"(
("`9ZZYWNjjY`Wcaaib]WUnjcb`UbX`Wc``UVcfUnjcb`g_]``g`]b`h\Y`WcbhYIh cZWfcgg!W`hifU``Wcaaib]miUbX`ai`nj!X]gWjd`]bUfmkcf_"	D9' "&ž'D9' "( ž'D9' "*
) "'G\ck'fYgdYWhZcf'Yh\]WU`'dfUWh]VW''UbX'gcVl]U`'fYgdcbg]V]`]hm'	D9' "%
*"'8 Ya cbglfUlY 'h\Y 'UV]']lmihc 'Yb[ U[ Y ']b ']bXYdYbXYbh'UbX 'fYZYWf]j Y 'YUfb]b[ "	D9' "' ž˙D9' ")

#### HYUWX]b[ 'GhfUhY[]Yg'

9 | dYf]Ybh]U``UbX`dfcV`Ya `VUgYX``YUfb]b[ `k ]```VY`h\Y`ZYUhi fY`cZh\]g`Wci fgY"'5g`U`Zci ft\ 'mYUf`Wci fgYžh\Y ZcW g`k ]```VY`cb`XYg][ b`UbX`fYgYUfW\`g\_]``gžWc``UVcfUh]cb`k ]h\]b`[ fci dg`UbX#cf`YI hYfbU``dUffbYfg f]bWi X]b[ `Wca a i b]hmUbX#cf`]bXi ghfmL

 $HYUWX]b[\ 'k\ ]```ZcW g`cb`dfcj\ ]X]b[\ 'gh XYbhg'k\ ]h \ 'gi \ ddcfh'hc ']bj \ Ygh][\ UhY \check{z}'UbU`mgY 'UbX`Yj U`i \ UhY 'Wca \ d`YldfcV`Ya ']b'U'\i a \ Ub]hUf]Ub Yb[\ ]bYYf]b[\ 'WcbhYlh' h'$ 

5 WUXYa ]Wg`]bj c`j YX`]b`h\]g`Wci fgY`UfY`YI dYWYX`hc`\Uj Y`gca Y`YI dYf]YbWY`]b`\i a Ub]hUf]Ub`Yb[ ]bYYf]b[ Y]h\Yf`h\fci [\`Z]Y`X`YI dYf]YbWYžfYgYUfW\`cf`hYUW\]b[ "'=bXi ghfma Ybhcfg`a UmVY`Uddc]bhYX`hc`ZI fh\Yf Ugg]ghik ]h\`h\]g"

# 5ggYgga Ybh

5ggYgga Ybh'hUg_	K Y][ \h	8i Y'8UHY	7 ci fgY @YUfb]b[ Ci HWca Yg 5ggYggYX
%"DfcYWi'cifbU`f%cZ&Ł	)	' \$#\$- #&\$&&`\$).\$\$`DA	%ž'&ž'' ž'( ž') ž'*
&"'DfcYWh'&i fbU`'f&'cZ&Ł	<b>%</b> \$I	&(#%#&\$&&`\$).\$\$`DA	%ž'&ž'' ž'( ž') ž'*
' "'A]X'Dfc^YWhDfYgYbhUh]cb	&) ı	&, #%\$#&\$&&`%%) - `DA	%ž'&ž'' ž'( ž') ž'*
("DfcYWh'∌hYfj]Yk	%) ।	% #%%#&\$&&`%%) - `DA	(Ž <sup>'*</sup>
)"DfcYWhfYdcfh	()	% #%%#&\$&&`\$).\$\$`DA	'Ž(Ž)Ž*

## 5ggYgga Ybh% Dfc YWh ci fbU f%cZ&L

8i Y'XUhY." \$#\$-#&\$&&"\$).\$\$"DA

K YY\_`m'ci fbU``XcW a Ybh]b[ ``YUfb]b[ 'UbX'cVgYf] Uh]cbgža YYh]b[ 'a ]bi hYg'UbX'dYfgcbU``fYZYW]cbg"`K YY\_ ' 'gi Va ]gg]cb']g'k cfh\')ı 'cZWci fgY'[ fUXY"'

 $A\ cW_i]bhYfj\ ]Yk\ 'VUgYX'cb'9B;\ ;\ (\%\&'dfc'YWhk\ ]h\ 'Yl\ dYfh']bhYfj\ ]Yk\ 'dUbY'''8Ya\ cbghfUh]cb'cZ'WYUf'dfc'YWha\ ubU[\ Ya\ Ybhg_]``gž'gi\ ghU]bYX']bj\ c`j\ Ya\ YbhXi\ f]b[\ 'hYfa' \ubX'fYZYWhj\ Y``YUfb]b[ 'cb'\i\ a\ Ub]hUf]Ub\ Yb[\ ]bYYf]b[ "$ 

H\]g^]g^bchU^Hi fb]hb^Ugg][ ba Ybh

5ggYgga Ybh). Dfc YWnfYdcfh

8i Y'XUhY.'% #%#&\$&&'\$).\$\$'DA

H\Y`Z\bU``fYdcfh`]g`U`gi a a UfmcZh\Y`[fci dfg`ci h\&a Yg`Zcf`h\Y`dfc`Y\\T\Y`fYdcfh`g\ci `X`VY`dfYdUfYX UbX\&f`YX]hYX`Ug`U`[fci d`UbX`dfcj]XY`U`\c`]gh]\Wgi a a UfmcZh\Y`dfc`Y\\T\J]a gžVU\\[fci bXž'fYgi `hg`UbX \\&b\M g]cbg\"`H\Y`\\bhf]\Vi h]cb`cZYU\\\`gh XYbh\r\h\Y`fYdcfh\k]```VY`UggYggYX`VmdYYfg`UbX`h\Y`U\\UXYa]\Wa Ybhcf\"

	5ggYgga Ybh	DfcYWhitifbU`f%cZ&Ł	
K YY_'(.'' 'C WhcVYf'!'+ C WhcVYf	@YWnifY	91 HYfbU``dUffbYf`Wcbgi `HUH]cbž`Z]bU`]gY dfYgYbHUH]cb`VUgYX`cb`dfY`]a ]bUfmfYgYUfW\`UbX d`Ub`Zcf`Z]bU``gi Va ]gg]cbg"	
	K cf_g\cd	DfchchmdY:XYg][ b:UbX:XYj Y`cda Ybh':	
K YY_'*.'%+'C WcVYf'!	@YWhifY	Bc'WUggYg']b'K YY_'*	
&%°CVVf	K cf_g\cd	Bc'kcf_g\cd']b'K YY_'*	
K YY_"+."&("C WhcVYf"! &, "C WhcVYf	@YWhifY	; Uh\Yf`ZYYXVUW_`Zfca `dfYgYbfUh]cb"`7cbh]bi Y`k]h\ dfc^YWf	
	K cf_g\cd	DfchchmdY:XYg][ bž:XYj Y`cda Ybh'UbX:hYgh]b[ "`	
	5ggYgga Ybh	A ]X`DfcYWhDfYgYbhUh]cb.`H\]g`]g`U`[ fci d dfYgYbhUh]cb`[ ]j Yb`ZJWY`hc`ZJWY`cb`WJa di g	
K YY_', .'' %C WvcVYf'!'( Bcj Ya VYf	@YWhifY	7 ca d`YhY`Z bU``dfcYWhghU[Yg`UbX`XfUZhifYdcfh'	
	K cf_g\cd	DfchchmdY XYg][ bžXYj Y`cda Ybh'UbX hYgh]b[ "	
K YY_''+'Bcj Ya VYf'! ‰Bcj Ya VYf	@YWhifY	DfYdUfY 'Zcf']bhYfj]Yk gž'gYY_'ZYYXVUW_'cb'fYdcfh XfUZrg"	
	K cf_g\cd	DfcchmdY`Z]bU`]gUh]cb`UbX`a Ubi U``dfYdUfUh]cb"	
K YY_'%\$.'%( 'Bcj Ya VYf	@YWhifY	Gi ghJ]bUV]`]hmUbX`Uddfcdf]UhYbYgg`cZgc`i h]cb"`	
!'% 'Bcj Ya VYf	K cf_g\cd	±bhYfj]Yk gʻfUggYgga Ybh']hYa Ł	
	5ggYgga Ybh	Dfc YWn ±ohYfj ]Yk	
	5ggYgga Ybh	Dfc Y WifYdcfh	
Gh XmK YY &% Bcj Ya VYf'! &( Bcj Ya VYf	5ggYgga Ybh	DfcYWititi fbU``f&'cZ&Ł	

### FYgci fW/g

#### DfYgWf]VYX F Ygci fWYg

5g'dfcj ]XYX'cb'A ccX'Y'

#### 7ci fgY 9j U`i Uh]cb UbX 8Yj Y`cda Ybh

: YYXVUW\_cb^h\Y`Wci fgY`]g`[Uh\YfYX`dYf]cX]WU``mi g]b[`j Uf]ci g`a YUbgž]bWi X]b[`h\Y`I BGK a m9I dYf]YbW'`dfcWYggž]bZcfa U``X]gW gg]cb`]b`h\Y`Z]bU``WUgg`Zcf`h\Y`Wci fgYž'UbX`h\Y`GW\cc`'g Ghi XYbh#GhUZZa YYh]b[`g"`Mci f`ZYYXVUW\_`]g`HU\_Yb`gYf]ci g`mž'UbX`Wcbh]bi U``]a dfcj Ya Ybhg`UfY`a UXY`hc`h\Y Wci fgY`VUgYXž']b`dUfhž'cb`gi W\`ZYYXVUW\_"

±0 'h\]g'Wci fgYžfYWYbh']a dfcj Ya Ybhg'fYgi `h]b[ 'Zfca 'ghi XYbh'ZYYXVUW\_']bWi XY'UX↑ gh]b[ 'h\Y'dfc YWi'ci fbU` hc'a cfY'YUg]`mWUdhi fY'ghi XYbh'`YUfb]b[ g"'

#### @UVcfUhcfmK cf\_g\cd \(\frac{1}{2}\)Zcfa Uhlcb

Ghi XYbhgʻk]``bYYX`hcʻWda d`YhY`A U\_YfgʻGdUWY`]bXi WhjcbʻUbX`hfU]b]b[ʻUgʻdUfhcZh\]gʻWci fgYž`]bZcffa Uhjcb hcʻVYʻdfcj [XYX`]bʻK YY\_'%''

## 5 WUXYa] W + DZcfa Uh]cb

: ]bU`'9I Ua ]bUh]cbg.

: ]bU``Yl Ua g`]b`H' `&\$&&k ]```VY`\Y`X`cb`]bY`VYlk YYb`&) h\`Bcj Ya VYf'!`, h\`8YWfa VYf`&\$&&`]bWi g]j Yž'UbX gi dd`Ya YbhJfmYl Ua g`VYlk YYb`-h\`!`% h\`>Ubi Ufm&\$&' `]bWi g]j Y"`Mci `UfY`fYei ]fYX`lc `VY`Uj U]`UV`Y`cb h\YgY`XUhYg"`D`YUgY`Xc`bchlc`a U\_Y`UbmdYfgcbU``cf`HfUj Y``UffUb[ Ya Ybhg`Xi f]b[ `h\]g`dYf]cX"`

57589A = 758J = 79

# 5ddYbX]l. '9b[]bYYfg'5i glfU`]U'f95Ł'DfcZYgg]cbU`'9b[]bYYf'7ca dYhYbWm GHJbXUfX

? bck `YX[Y'UbX'g_]```VUgY  D9%%7ca dfY\Ybg]j Yž'h\YcfmVUgYX'i bXYfgHJbX]b['cZh\Y'i bXYfd]bb]b['bUhi fU`'UbX d\mg]\WJ`'g\WJYb\W'g'UbX'h\Y'Yb[]bYYf]b['Z bXUa YbHJ`g'Udd`]\WJV`Y'hc'h\Y'Yb[]bYYf]b[''	
D9%"%7ca dfY\Ybg]j Yž'h\YcfmVUgYX'i bXYfgHJbX]b['cZh\Y'i bXYfd]bb]b['bUh fU`'UbX d\mg]WJ`'gW]YbW'g'UbX'h\Y'Yb[]bYYf]b['Z bXUa YbHJ`g'Udd`]WUV`Y'hc'h\Y'Yb[]bYYf]b[''	