

# **CVEN3203**

# 7ci fgY Cj Yfj ]Yk

#### GHJZ:7cbHJWh'8YHJ]`g

#### 7cbj Ybcfg

B Ua Y	9a U]`	5j U]`UV]`] <b>m</b>	@cWJhjcb	D\cbY
8f?ifh8ci[`Ug	_"Xci [`Ug4 i bgk "YXi "Ui	H67 <sup>-</sup> ]b WUgg	79°)\$*	-',) ') \$(*

#### @YWhi fYfg

B Ua Y	9a U]`	5j U]`UV]`]m	@cWJhjcb	D\cbY
8f.6UVU_	V"g\U\VcXU[\4 i bgk "YXi "Ui	H67 <sup>-</sup> ]b WUgg	79')\$+	
$G\U\VcXU[\L]\Ub$	_			

#### GWXcc~7cbhJWh~abZcfa Uhlcb

<u>9b[]bYYf]b['Ghi XYbhGi ddcfhGYfj]WYg'-</u>'H\Y'Bi WYi g'!'Ybfc`a Ybhž'dfc[fYgg]cb'W\YW\_gž'W`Ug\'fYei Yghgž Wci fgY']ggi Yg'cf'dfc[fUa!fY`UhYX'ei Yf]Yg'

<u>9b[]bYYf]b[ '±0Xi ghf]U' 'HfU]b]b[</u> '-'±0Xi ghf]U' 'hfU]b]b[ 'ei Ygh]cbg'

LBGK Gh Xm5VfcUX - gh XmUVfcUX gh XYbhYbei ]f]Yg fZcf ]bVci bX gh XYbhgŁ

<u>I BGK '91 WXUb[Y</u>'-'gh XYbhYl WXUb[Y'Ybei]f]Yg'flcf']bVci bX'gh XYbhgŁ'

LBGK : i h fy Gh XYbh - dch bh U gh XYbh Ybei ]f]Yg Y"[" UXa ]gg]cbgž ZYYgž dfc[fUa gž WfYX]h lf UbgZYf

#### D\cbY.

fŽ\*%'&Ł'-',)',)\$\$'-BiWYig'GhXYbh<iV'

fŽ\*%%&£'-',) '+\*\*%'-'9b[]bYYf]b['=bXi ghf]U`'HfU]b]b['

fŽ\*%%&L-',) " %+- '-1 BGK 'Gh Xm5VfcUX'UbX'I BGK '91 WXUb[Y'fZcf']bVci bX'gh XYbhgL'

# 7ci fgY 8YHJ] g

#### 7 fYX]h'Dc]bhg'\*

#### Gi a a UfmcZh\Y 7ci fgY

#### 7 ci fgY 5]a g

#i]g'Ub'U]a 'cZh\]g'Wti fgY'hc'\Y`d'XYj Y`cd'h\Y'Zc``ck ]b['[fUXi UhY'Uhff]Vi hYg.Hc'[]j Y

ghi XYbhgʻUʻgc`]Xʻ[ fUgdʻcZh\Yʻh\YcfmUbXʻdfUWf)WYʻcZ[ YchYVXb]WU`Yb[ ]bYYf]b[ žʻUbXʻhcʻVYʻZJa ]`]Ufʻk ]h\ʻh\Y VUgYgʻcZfYgYUfVXʻhcʻZ fh\Yf`XYj Y`cdʻ]hgʻhYWXbc`c[ m'ʻ\bʻUXX]h]cbžʻ[ fUXi UhYgʻg\ci `X'VYʻUV`YʻhcʻUdd`mih\Ycfm hc

dfuWjWr]b ZJa ]`]Uf UbX i bZJa ]`]Uf g]h Uhjcbg/

 $\label{thm:continuity:continuity:boly:contin$ 

Hc'hYUW\'ghi XYbhg'\ck 'hc'XYZ|bYž'UbU`mgY'UbX'gc`j Y'dfcV`Ya g'WYUf'm'UbX``c[]\WJ``m'UbX']b'Xc]b['gc'VYUV`Y'hc'Z|bXžYj U`i UhYž]bhYfdfYh'UbX'Wc``UhY']bZcfa Uh]cb/

 $\label{thm:likelike} He `XYj Y`cd'] b XYdYb XYbh Wf] h W ``h ci [ hk ]h ]b `gh XYbhg `gc'h Uhk Yb `bYWfgg Ufmih Ymk ]``VY'UV'Y'hc W U``Yb[Y'W ffYbh_bck `YX[Y'UbX'h]b_]b[/$ 

 $\label{thm:deca} He'dfca\ ch' U'fYgdYWhk\ ]h\ ]b'ghi\ XYbhg'Zcf']bX]j\ ]Xi\ U``\ a\ Ub'f][\ \hg'UbX'X][\ b]hmž'dUfh]Wi\ `Uf'mik\ Yb']hfY`UhYg\ hc'a\ Ya\ VYfg'cZh\Y'di\ V']Wcf'ch\Yf'dYcd'Y'k\ \c'k\ ]```VY'UZZYWhYX'Vmih\Y'dfc'YWg'h\Uhih\YmXYg][\ b'UbXYIYW'hY/$ 

Hc ZcghYfYZYWhj Y gY`Za UbU[Ya Ybhg\_]``g/

Hc'bi fhi fY'h\Y'g\_]``g'fYei ]fYX'Zcf'YZYWfj Y``YUXYfg\]d']bWi X]b[ 'Ub'UV]`]hmhc'a UbU[Y'UbX'XY`]j Yf'dfc'YWfgž Ub'i bXYfghUbX]b[ 'cZh\Y'gc\]U``XmbUa ]\Wg'cZ[ fci d'dYfZcfa Ub\W'ž'U'fYdYfhc]fY'cZdfc\W'ggYg'Zcf'h\Y YZY\Wfj Y'a UbU[Ya YbhcZ[ fci dgž'UbX'h\Y'UV]`]hmhc'j U`i Y'X]j YfgY'\U\W\_[ fci bXg'UbX'cd]b]cbg'UbX'Z b\Wjcb YZY\Wfj Y`m']b'a i `h\X]g\\Jd\]bUfmhYUa g/UbX

Hc']a dUffigci bX'\(\pm\)'k cf\_]b['g\_]\`g"

## 7ci fgY @YUfb]b[ Ci hWca Yg

5 ZHY figi WWY ggZi ``miWca d`Yhjb[ ih\]giWci fgYžmci ig\ci `XiVYiUV`Yihc.

#### 5XX]h]cbU`7ci fgY \=bZcfa Uh]cb

;  $YchYVXb]WU^9b[]bYYf]b[^]g'hY'gh XmcZhY'VY\Uj]ci f'cZgc]`žfcW_'UbX'[fci bXk UhYf'i bXYf'Yb[]bYYfYX Ybj]fcba Ybhg''A cghYb[]bYYf]b[^ghf Wh fYg'k]^*]bYj]hUV`m\Uj Y'gca Y'gcfhcZ]bhYfUWf]cb'k]h\'h\Y'[fci bX gi fZUWY'''; YchYVXb]WU^9b[]bYYfg'UhYa dhhc'XYgWf]VY'UbX#cf'a cXY`'h\]g']bhYfUWf]cb'hc'UWX]Yj Y'U'gUZY'UbX YZJW]YbhXYg][b''$ 

Gc ZJfžmci `\Uj Y ghi X]YX 7 J 9 B ' &\$& `Gc]``A YW\Ub]Wg"'H\YfYZcfYž'Vmbck `mci `g\ci `X`i bXYfghUbX.`h\Y VUg]WYb[]bYYf]b[ `WUgg]ZJ\Uh]cb `cZgc]`/\ck `gc]``VY\Uj Yg`i bXYf`]a dcgYX`ghfYggYg`UbX`ghfU]bg/UbX`\ck [fci bXk UhYf`Zck g`h\fci [\`gc]``UbX`]\mathbf{g}`YZZYWhcb`Yb[]bYYfYX`ghfi Whi fYg"'H\YfY`UfY`hk c`a U]b`UfYUg`h\Uh mci `\Uj Y`bchWcj YfYX`h\Uhk]``VY`UXXfYggYX`]b`h\]g`Wci fgY.

fbł<ck 'hc 'fY`UhY 'h\Y 'fYU`!k cfX'' [Yc`c[]\WJ``Ybj]fcba Ybhhc 'mci f'\_bck `YX[Y`cZ'\WUgg!fcca '`gc]`/UbX fbł<ck 'hc '\ka V]bY 'mci f' W ffYbh\_bck `YX[Y`UbX`DUfhfbł:hc 'dYfZcfa 'U'; YchY\\b]\WJ``9b[]\bYYf]b[ 'XYg][b"

#### DUfhfbŁ9b[]bYYf]b[; Yc`c[m

 $5 \text{ ``, YchYW.b]WD``9b[]bYYf'a i gh\Uj Y`Ub`i bXYfgHUbX]b[`bchcb`mcZYb[]bYYf]b[`df]bW]d`Yg`Vi hU`gc`cZ [Yc`c[mUbX'h\Y`]b\YfYbhj Uf]UV]`]hmUbX`W.U``Yb[Yg`]h\Ug`ZcfYb[]bYYf]b["'H\]g`Wci fgY`k]``hYUW`mci `UVUg]Wi bXYfgHUbX]b[`cZ[Yc`c[m]bWi X]b[`\ck `[YchYW.b]WD``a UhYf]U`g`UfY`Zcfa YXžk\Uhih\Y]f \\ UfUWhYf]gh]Wg`UfY`UbX`\ck `hc`XYgWf]VY`h\Ya`i g]b[`Yb[]bYYf]b[`UbX`[Yc`c[]]WD``hYfa g"'\dik ]``UhfYa dhhc []j Y`mci `gca Y`i bXYfgHUbX]b[`cZh\Y`W.U``Yb[Yg`U'[Yc`c[]]WD``Ybj]fcba Ybha Um\Uj Y`Zcf`U`dUfh]Wi`Uf Yb[]bYYf]b[`dfc`YWh`5hh\Y`YbX`cZh\Y`Wci fgY`mci `g\ci `XžZcf`Ubmg]hY`UbX`Yb[]bYYf]b[`dfc`YWhzVY`UV`Y`hc Y]h\Yf.`fUEXYj Y`cd`U`dfY`]a ]bUfm[YchYW.b]WD``a cXY``Zcf`h\Y`g]hY`h\Uh\Wb`VY`i gYX`Zcf`XYg][b`cf`fVEVY UV`Y`hc`X]gWi gg`a cfY`Wca d`YI`[Yc`c[mk]h\`9b[]bYYf]b[`; Yc`c[]ghg`hc`U[U]b`Wca Y`i d`k]h\`U`gi]hUV`Y [YchYW.b]WD``a cXY``Zcf`h\W.b]WD``a cXY``Tcf`h\Y`g]hY`h\Uh\Wb`VY`i gYX`Zcf`XYg][b`cf`fVEVY UV`Y`hc`X]gWi gg`a cfY`Wca d`YI`[Yc`c[mk]h\`9b[]bYYf]b[`; Yc`c[]ghg`hc`U[U]b`Wca Y`i d`k]h\`U`gi]hUV`Y [YchYW.b]WD``a cXY``$ 

#### DUfhfbl:5dd^]YX; YchYW.b]Wg

H\]g`dUfficZh\Y`Wci fgY`fYdfYgYbhg`h\Y`'Z]bU``ghU[Y'`cZU; YchYW\b]\WJ``dfcYWf'`\dik]```fYei]fY`mci `hc`ghi Xm h\Y`Wcbj Ybh]cbU``a Yh\cXg`Zcf`h\Y`XYg][b`UbX`UbU`mg]g`cZWca a cb`[YchYW\b]\WJ``Wcbghfi Wf]cbg`]bWi X]b[g\U``ck``UbX`XYYd`fd]`Y\&Zci bXUh]cbg`UbX`fYhU]b]b[`k U``g"': cf`a UbmcZmci žh\]g`k]```VY`mci f`Z]bU``Wci fgY`]b; YchYW\b]\WJ``9b[]bYYf]b[`UbX`k Y`\cdY`mci `[U]b`Ub`UddfYW]Uh]cb`cZgca Y`cZh\Y`Wca d`YI]h]Yg`cZ; YchYW\b]\WJ``9b[]bYYf]b["

H\cgYž'bc'Xci Vh'UHfUWij Y'UbX'\][\m]bH'``][Ybhghi XYbhgž'cc\_]b['Zcf'U'XYa UbX]b['UbX'W.U`Yb[]b['mYh j YfmgUhgZmb['WUfYYf'k]```cVj ]ci g`mk ]g\'hc'di fgi Y'; YchYW.b]WU``9b[]bYYf]b['Z fh\Yf''K Y'\Uj Y'U'bi a VYf cZ; YchYW.b]WU`'YYWij Yg']b'Z]bU``mYUf'h\Uhk]```YI hYbX'mci f'\_bck `YX[Y'Yj Yb'Z fh\Yf']bhc'UfYUg'`]\_Y UXj UbWX'gc]``a YW\Ub]Wg/Udd`]WUh]cbg'cZWca di hYf'g]a i `Uh]cb'hYW\b]ei Yg'hc'[YchYW.b]WU``Yb[]bYYf]b[ dfcV'Ya g/[fci bX']a dfcj Ya YbhUbX'h\Y'XYg][b'cZdUj Ya Ybhgž'h bbY`g'UbX'g`cdYg'''7 ca Y'UbX'hU`\_'hc'i g']Z mci 'k Ubhhc'\_bck 'a cfY''

5g'U'[fUXi UhY'; YchYWkb]WU``9b[]bYYfz'mci 'a ][\hYl dYWh'nc'k cf\_'cb'dfc'YWg'Ug'X]j Yfg]Z]YX'Ug.'Vi ]'X]b[UbX'Vf]X[Y'Zci bXUh]cb'XYg][b'Xua 'XYg][b'UbX'Wcbglfi Wf]cb/fcUX'dUj Ya YbhXYg][b/g`cdY'gHUV]`]muUbU`mg]g'UbX'gHUV]`]gUh]cb/UbX'h bbY``UbX'a ]bY'XYg][b''A cghimd]WU``mimci 'k ]```Xc'U'dUffhha Y'Wci fgYk cf\_a UghYfg'k ]h\i g'UzhYf'k cf\_]b['Zcf'U'mYUf'cf'hk c'hc'gi dd`Ya Ybhimci f'\_bck 'YX[Y'fUbX'dfcj ]XY'Ub'YI W gY Zcf'mci f'\][\'W\Uf[Y!ci hfUhYt''Gca Y'cZmci 'a UmYj Yb'k ]g\'hc'Xc'U'D\8'f]Z]bhYfYghYX'Wca Y'UbX'hU`\_'k ]h\i g'Ubmha Yzk Y'\Uj Y'`chg'cZdfc YWg#gWXc`Ufg\]dg'Uj U]`UV'Yt''

5ggYgga Ybh

a Uf\_g"'G][ b]ZJWUbhdUfhJU``Wca d`YhJcbž'\U`Za Uf\_g"

 $A\ Uf\_]b[\ ^{k}]^{``c}CVWV\ f^{`}Xi\ f]b[\ ^{Y}UVVX\ ^{k}\ cf\_g\\ \ cd"$ 

5ggYgga Ybh&; Yc`c[mEi]n

GhUfh:XUhY. '&-#\$' #&\$&%'\$\*.\$\$'DA

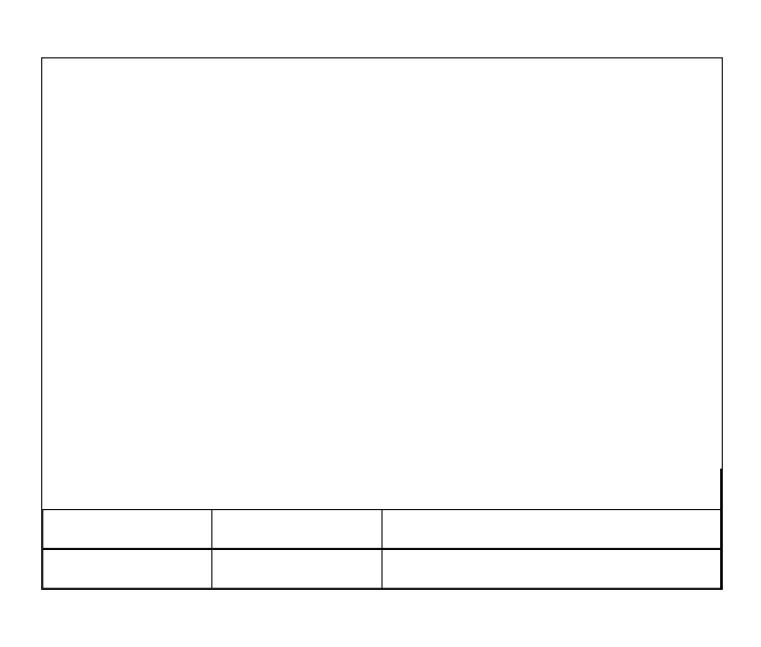
**@Yb[h**...%\cif.%) a ]bg

8YHJ]`g.

; Yc`c[mei]n'k]``'VY'WcgYX'Vcc\_'UbX'k]``'hYghi bXYfglUbX]b['cZh\Y'[Yc`c[mWcadcbYbhcZh\Y'WcifgY"

#### 5XX]h]cbU`XYhU]`g.

 $F Y Y U g Y U b X 'g i Va ] g g ] c b `c Z h X 'e i ] n `k ] `` V Y 'j ] U `A c c X `Y "`A U f \_g `U f Y `Y I d Y W f X `h c `V Y `f Y h f b Y X `k ] h ] b `' k Y Y \_g `c Z g i Va ] g g ] c b "$ 



F Ygci fWYg

DfYgWf]VYX F Ygci fWYg

gua d`]b[ 'cZg]hYg'k ]h\ 'dchYbhJu``mWcbhJa ]bUhYX'gc]`'! 'Bcb!j c`UhJ`Y'UbX'gYa ]!j c`UhJ`Y'Wca dci bXg

## ]D\cbY`fUbX`ch\Yf`U`a cgh`Ug`ga Ufh`d\cbYgŁ

H\YfY`UfY`bi a Yfci g`Uddg`VY]b[ `XYj Y`cdYX`Zcf`j Uf]ci g`ga Uffid\cbYg"`5hh\Y`a ca Ybhzh\YfY`UfY`cb`mU\UbXZ ``XYj Y`cdYX`Zcf`[ Yc`c[ mh\UhUfY`ZfYY"`A UbmcZh\Y`cbYg`Zcf`)



# Gi Va ]gg]cb cZ5ggYgga YbhHUg\_g

 $D`YUgY`fYZYf`hc`h\Y`A ccX`Y`dU[Y`cZh\Y`Wci fgY`Zcf`Z ff\Yf`[i]XUbWY`cb`UggYgga Ybhigi Va]gg]cb" \\$ 

## 5 WUXYa ]W<cbYghmUbX D`U[ ]Uf]ga

6Yk UfY "5 b 'Ugg][ ba Ybhih Uh]bWi XYg 'd `U[ ]Uf]gYX 'a UhYf]U` 'k ]```fYWY]j Y 'U`\$ı : U]`ž 'UbX 'ghi XYbhg 'k \c d`U[ ]Uf]gY 'UfY 'U`gc '`]UV`Y 'hc 'X]gW]d`]bUfm'UWf]cbž ]bWi X]b[ YI Wi g]cb 'Zfca 'Ybfc`a Ybh'

D`U[]Uf]ga `]g`h\Y`i gY`cZUbch\Yf`dYfgcb'g`k cf\_`cf`]XYUg`Ug`]Zh\Ymk YfY`mci f`ck b"`K \Yb`]h`]g`bYWYggUfmcf XYg]fUV`Y`hc`i gY`ch\Yf`dYcd`Y'g`a UhYf]U``mci 'g\ci `X`UXYei UhY`mUW\_bck `YX[Y`k \cgY`k cfXg`cf`]XYUg`h\Ym UfY`UbX`k \YfY`mci 'Zci bX`h\Ya 'f[]j ]b[ 'h\Y`Wca d`YhY`fYZYfYbWY`XYhU]`gž`]bWi X]b[ 'dU[Y'bi a VYff'g\t\"H\Y @YUfb]b[ '7 YbhY'dfcj ]XYg`Z fh\Yf`]bZcfa Uhcb`cb`k \UhWcbgh]hi hYg`D`U[]Uf]ga 'Uh

\hdg.#ghi XYbh'i bak "YXi "Ui #d`U[]Uf]aa

# 5ddYbX]l. '9b[]bYYfg'5i glfU`]U'f95Ł'DfcZYgg]cbU`'9b[]bYYf'7ca dYhYbWm GHJbXUfX

Dfc[fUa '±bHYbXYX'@YUfb]b['CiHWca Yg	
?bck `YX[Y'UbX'g_]```VUgY	
D9%%7ca dfY\Ybg]j Yžh\YcfmVUgYX'i bXYfghUbX]b[ 'cZh\Y'i bXYfd]bb]b[ 'bUhi fU`'UbX d\mg]\WJ`'g\WJYb\Wg'UbX'h\Y'Yb[ ]bYYf]b[ 'Z bXUa YbhU`g'Udd`]\WJV`Y'hc'h\Y'Yb[ ]bYYf]b[ 'X]g\WJd`]bY	
D9%"&"7cbWfdhiU``ibXYfghUbX]b['cZh\Y'aUh\YaUh]WgžbiaYf]WU``UbU`mg]gžghUh]gh]Wgž'UbX WcadihYf'UbX']bZcfaUh]cb'gW]YbWYg'k\]W\ibXYfd]b'h\Y'Yb[]bYYf]b['X]gW]d`]bY	
D9%" '±b!XYdh\'i bXYfgHJbX]b[ 'cZgdYW]U`]ghVcX]Yg'cZ_bck `YX[ Y`k ]h\]b'h\Y'Yb[ ]bYYf]b[ X]gW]d`]bY	
D9%'( '8]gWYfba YbhcZ_bck `YX[ Y`XYj Y`cda YbhUbX`fYgYUfW\ X]fYWIjcbg`k ]h\]b`h\Y Yb[ ]bYYf]b[ 'X]gWJd`]bY	
D9%) '? bck `YX[Y`cZYb[]bYYf]b[ 'XYg][b'dfUWf]WY'UbX'WcbhYl hi U``ZUWcfg']a dUWf]b[ 'h\Y Yb[]bYYf]b[ 'X]gW]d`]bY	
D9%"* I bXYfgHJbX]b[ 'cZh\Y 'gWcdYždf]bW]d`Ygžbcfa gž'UWWci bHJV]`]h]Yg'UbX'Vci bXg'cZ gi gHJ]bUV`Y'Yb[ ]bYYf]b[ 'dfUWf]WY']b'h\Y 'gdYW]ZJWX]gW]d`]bY	
9b[]bYYf]b['Udd']WUh]cb'UV]']m	
D9&"%5dd`]\Wlr]cb`cZYgHJV`]g\YX`Yb[]bYYf]b[`a Yh\cXg`hc`Wca d`Yl `Yb[]bYYf]b[`dfcV`Ya gc`j]b[	
D9&"&": `i YbhiUdd`]WUh]cb'cZYb[]bYYf]b['hYWXb]ei Ygž'hcc`g'UbX'fYgci fWfg	
D9&"' '5dd`]WUh]cb'cZgmghYa Uh]WYb[]bYYf]b['gmbh\Yg]g'UbX'XYg][b'dfcWYggYg	
D9&"('5dd`]\WJr]cb`cZgmghYaUh]\WUddfcU\\XYg`hc`h\Y`\\cbXi\WiUbX`aUbU[YaYbhcZYb[]bYYf]b[dfcY\\mathred{Wg}	
DfcZYgg]cbU``UbX`dYfgcbU``Ultf]Vi H/g	
D9' "%'9h\]WU``W&bXi WhUbX`dfcZYgg]cbU``UVW&i bHJV]`]hm	