

ARTS4266

Di nn`Ygž'D`Ubb]b[ž'UbX'DfYgYbhUh]cb'Zcf'<cbci fg']b'h\YGcW]U`'GW]YbWYg

HYfa 'C bY''# '&\$&\$

7ci fgY⁻Cj Yfj]Yk

'GhJZZ'7cbhJWh'8YhJ]`g'

'7cbj Ybcfg'

B Ua Y	9a U]`	5j U]`UV]`] m	@cWUh]cb	D\cbY
G]cV\Ub^Cf&i ``]j Ub	g]cV\Ub"cgi ``]j Ub4 i bgk "YXi "Ui		‰* ž'A cfj Yb 6fck b	-',)'\$*,-

GWXcc`7cbHJWhi±bZcfa Uhjcb

GWXcc``cZGcWJU``GWJYbWYg

Fcca '%) -

A cfj Yb 6fck b 7 &\$

Ya U]`. 'gcgg4 i bgk "YXi "Ui

d\cbY. '\$&'-',) '% \$+

7ci fgY 8YHJ] g

7 fYX]hDc]bhg *

Gi a a UfmcZh\Y 7ci fgY

H\]g']g'U'Wca di `gcfmWci fgY Zcf'GcWJU`GWJYbW'g`\cbci fg'ghi XYbhg`]b'h\Y'GW\cc`cZGcWJU`GWJYbW'g" \= k]```]b'ffcXi W'mci 'hc'h\Y'dfUWJW'cZh\Yg]g'k f]h]b['UbX'gi ddcfhmci ']b'h\Y'YUf'mghU[Yg'cZXYj Y`cd]b[mci f`\cbci fg'Uf[i a Ybh'H\]g'Wci fgY']bWi XYg'hcd]Wg'gi W. 'Ug.'i g]b['`]VfUfmfYgci fW'g'Zcf`\cbci fg ghi XYbhg`]bWi X]b['fYgYUfW. 'Wcbgi `hUhjcb'UbX'UWW'gg'hc'XUhUVUgYg/h\Y'fc'Y'cZa Yh\cXg']b'fYgYUfW. 'UbX h\Y'i gY'cZh\Ycfm]b'ZfUa]b['UbX'WcbXi WJb['U'fYgYUfW. 'dfc'YWi]b'h\Y'gcWJU`'gWJYbW'g/mci f'Yh\]WU` fYgdcbg]V]`]hJYg'Ug'UfYgYUfWX'd'Ubb]b['UbX'a UbU[]b['U'fYgYUfWX'dfc'YWW'k cf_]b['YZYWJj Y`mk]h\mci f'gi dYfj]gcf/hja Y'UbX'XUhU'a UbU[Ya Ybhg_]``g"'H\Y'Wci fgY']b'ffcXi W'g'mci 'hc'h\Y']XYU'cZZfUa]b[mci f'fYgYUfWX'Ug'Ub']bhYfj YbhJcb']b'U'X]gWJd`]bUfmXYVUhY'fcf'gYfJYg'cZXYVUhYgb'''5 'dUffJW'`Uf'ZcW'g'cZU a]bcf!h\Yg]gž'UbX'h\]b_]b['UVci h\\Y'h\Yg]g'Zcfa "'H\]g']bWi XYg'`YUfb]b['UVci h\\Y'Wca dcbYbhdUffg'cZU a]bcf!h\Yg]gž'UbX'h\]b_]b['UVci h\\ck' mci 'a][\hWcbg\fi Whmci f'ck b'h\Yg]gž'Zcfa UI]a i a ']a dUWf'

7 ci fgY @YUfb]b[Ci hWca Yg

- %" ⇒XYbhZmh\Y`ZYUhi fYg`cZUb`ci hqhUbX]b['h\Yq]g`cf`X]ggYfhUh]cb"'
- &" J YfVU``mdfYgYbha UhYf]U``]b'Ub'Yb[U[]b['UbX']bZcfa Uh]j Y'k Um'
- '" K cf_'Wc``UVcfUhjj Y`mik]h\"Wc``YU[i Yg'hc'g\UfY'g_]``g'UbX'_bck `YX[Y'fY`Yj Ubh'hc'dfcXi Wjb['U'a]bcf h\Yg]g

HYUWX]b[GhfUhY[]Yg

 $\label{thm:continuity} $$H^{\gamma}_b H^{\gamma}_j Y^k \ cf_g \ d'U^ck g'mci 'hc'[Yhk \ cf_]b['cb'mci f'fygYUfW'dfc YWg'ei]W_m''+i]g'XYg][bYX'hc Vch'gi ddcfhmci ž'UbX'hc'YZ]Wfbhm]bfcXi W''mci 'hc'h\Y'_Ymd]YWg'cZ_bck 'YX[Y'mci 'k]''bYYX'hc Wca d'YhY'mci f'\cbci fg'mYUf''H\]g']bWi XYg']bZcfa Uhjcb'cb'h\Y'Yh\]WU''Udd']WUhjcb'dfcWfggž'XUhU'ghcfU[Yžk cf_]b['k]h\'U'gi dYfj]gcf'UbX'']VfUfmfYgci fWfg''H\Y'UggYgga YbhZcW'g'k]'''VY'cb']XYbhJZm]b['YI WY''YbW'']b'h\Yg]g'k f]h]b['Vch\'h\Y']f'Yhhif fYž'UbX'dUgh\cbci fg'h\YgYg'''Nci 'k]''''U'gc'g\UfY'h\Y]f YI dYff]gYžk]h\'ch\Yfg']b'h\Y'WUggžj]U'mci f'[fci d'dfYgYbhUh]cbg'''8]ZYfYbhdfYgYbhUh]cbg'k]''''VY'ZcW'gYX cb'X]ZYfYbhY'Ya Ybhg'cZU'a]bcf'h\Yg]g'''$

5ggYgga Ybh

D`YUgY`gYY`A ccX`Y`Zcf`Z```]bZcfa Uhjcb`UVci hh\Y`UggYgga Ybhg"`

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7 'Ugg'; i]XY'! 'VUgYX'cb dfYgYbfUf]cb'	%\$ı	%(#\$(#&\$&\$`\$&.\$\$`DA	,

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GhUfh'XUhY.

@Yb[h\.'&ž)\$\$

 $8YHJ)^*g. "Ghi XYbhg'k]"^k f]hY'U'&z) $$^k cfX'YggUmZcW gYX'cb']XYbhJZm]b["UbX'YI d`cf]b["h\Y'ZYUhi fYg'cZUb ci hgHJbX]b["fYgYUfW.'X]ggYfHJhJcb"'K f]hHYb'ZYYXVUW_"UbX'U'bi a Yf]WJ''[fUXY'k]"^VY'fYhi fbYX'k]h\]b hk c'k YY_g'cZXY']| Yfm'$

Hi fb]h]b'gYh]b[.'H\]g'Ugg][ba Ybh]g'gi Va]hhYX'h\fci [\'Hi fb]h]b'UbX'gh XYbhg'Xc'bchgYY'Hi fb]h]b g]a]'Uf]hmfYdcfhg"

5ggYgga Ybh&; fci d dfYgYbhJh]cb

Ghufh Xuhy.

@Yb[h\."\$a]bihYcfU`dfYgYbhUh]cb

8 YHJ]`g. K cf_]b[']b'[fci dgžghi XYbhg`k]```dfYgYbhih\Y`fYghcZh\Y`WUgg`k]h\ 'h\Y]f`'UbU`mg]g`cZk \Uh Wcbghjhi hYg`Ub`ci hgrUbX]b['h\Yg]g"`K f]hhYb`ZYYXVUW_'UbX`U`bi a Yf]WU``[fUXY`k]```VY`fYhi fbYX`k]h\]b kk c`k YY_g`cZXY`]j Yfm''; fUX]b[']g`Wc``YWf]j Y"

5ggYgga Ybh' . 7`Ugg; i]XY! VUgYX cb dfYgYbhUh]cb

GhUfh'XUhY.

8 YHJ]`g. '9 UW\ [fci d`fl/UgYX`cb`h\Y`dfYgYbHUh]cb`[fci dgŁ'k]```dfcXi W/`U`%\$\$\$`k cfX`[i]XY`Zcf'h\Y]f WUgga UhYg`fh\cgY`a Ya VYfg`cZh\Y`WUgg`k \c`X]X`bchdfYgYbhk]h\`h\Y`[fci dŁ"'H\Y`[i]XY`k]```U]X`h\Y`fYgh cZh\Y`WUgg`]b`h\Y]f`h\Yg]g`dfYdUfUh]cb`k cf_"`K f]hYb`ZYYXVUW_UbX`U`bi a Yf]\W\``[fUXY`k]```VY`fYhi fbYX k]h\]b`hk c`k YY_g`cZXY`]j Yfm''; fUX]b[`]g`Wc``YWfj Y"H\]g`]g`h\Y`Z]bU``UggYgga YbhZcf'h\]g`Wci fgY"

li fb]h]bˈgYh]b[. H\]gʻUgg][ba Ybh]gʻgi Va]h\YX`h\fci [\'Hi fb]h]bʻUbXʻgh XYbhgʻXcʻbchgYY`Hi fb]h]a]`Uf]hmfYdcfhg"	j b

5 https://bxubwww.Fyei]fya Ybhg

D`YUgY`bchY`h\Uh`YWh fY`fYWcfX]b[g`UfY`bch'Uj U]`UV`Y`Zcf`h\]g`Wci fgY"`Ghi XYbhg`UfY`ghfcb[`mYbWci fU[YX`hc UhhYbX`U```WUggYg`UbX`WcbhUWh\Y`7 ci fgY`5i h\cf]hmhc`a U_Y`U`hYfbUh]j Y`UffUb[Ya Ybhg`Zcf`WUggYg a]ggYX"

7 ci fgY GWX YXi `Y

J]Yk Wugg'ha Yhuv'y

H]a YHJV`Y

8 UhY	Hmd Y	7 c bhYbh	
K YY_'% '%+': YVfi Ufm'! '&%	GYa]bUf		&da '-'(da
: YVfi Ufm		K YY_'%'!	K Y`Wca Y
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	' "'K \Yb'XcYg']bghh hjcbu'Yh\] Uddfcj U''bYYX'hc'VY'cVhU]bYX3 ("'H\Y'I BGK 'F YgYUfW\'7 cXY (da '- *da H\Yg]g'9'Ya Ybh' . 'K \Uh]g'a ']hYfUh fYfgŁ3 %"'K \m]h]g'bYWYggUfmhc'WcbX ']hYfUh fY'fYj]Yk &"':]bX]b['h\Y'']hYfUh fYfgŁ'mci ' "'Di fdcgYZ ``fYUX]b['cZh\Y'']h ("'7 fYUh]b['Ub'UbbchUhY'V]V`]c[) "'-₺Wi g]cb'UbX'YI Wi g]cb'Wf]h mci f'']hYfUh fY'fYj]Yk	i WiU bYYX fUd\m
K YY_') .'%* 'A UfWX '! '&\$ A UfWX	&da ''(da (YY') '- Hi Yg	

			%"'⇒XYbh]Zm]b['dUhhYfbg']b'Yj]XYbWY &"' <ck'hc'ghfiwhify'mcif'z]bx]b[g< th=""></ck'hc'ghfiwhify'mcif'z]bx]b[g<>
			"' <ck'hc'wcaaib]wuhy'ncif'z]bx]b[g'hc h\Y'fYUXYf</ck'hc'wcaaib]wuhy'ncif'z]bx]b[g'hc
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K YY_``% `5df]`!`%+ 5df]`	GYa]bUf	K YY_'- '- Hi Yg 5df]`'%(&da '- (da H\Yg]g'9`Ya Ybh'*. 'Gc'k\Uh3'fmci f X]gW' gg]cb'UbX'WcbWi g]cbgŁ' %"8YjY`cd]b['h\Ycfm'
			&"'K\Yb`]g`]hbYWYggUfmhc'dfYgYbh bYk'h\Ycfm3
			' "' <ck 'hc'fy`uhy'mci="" f'z bx]b[g'vuw_'hc<br="">h\Y'Y]gh]b['`]hYfUhi fY"</ck>
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			(da ''*da
			7`Ugg`dfYgYbhUh]cbg.
			(da '-'(" \$da '9'Ya Ybh%'K \Uh]g'a m fYgYUfW\'ei Ygh]cb3
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FYgci fWfg

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5```fYUX]b[g'k]```VY`]b'@Y[Ubhc"'9bhYf'j]]U'AccX`Y"'

FYWca a YbXYX FYgci fWYg

5```fYUX]b[g'k]```VY`]b'@Y[Ubhc"'9bhYf'j]]U'AccX`Y"'

7 ci fgY '9j U'i Uh]cb 'UbX '8Yj Y`cda Ybh

Mci f'ZYYXVUW_k]``'VY'i gYX'hc'i dXUhYX'`YWh fY'hcd]Wg'UbX'UggYgga Ybhg'''

Gi Va]gg]cb cZ5ggYgga YbhHUg_g

Gi Va]gg]cb cZ5ggYgga YbhHUg_g

Hi fb]h]b Gi Va]gg]cb

⊋mci 'YbWci bhYf'U'dfcV'Ya 'k \Yb'UhhYa dh]b['hc'gi Va]h'mci f'Ugg][ba Ybh'h\fci [\'Hi fb]h]bž'd'YUgY

5 WUXYa | W < cbYghmUbX D`U[| Uf]ga

D`U[]Uf]ga i]gii g]b[ih\Yik cfXgicfi]XYUgicZch\YfgiUbXidfYgYbh]b[ih\Ya iUgimci fick b"i±iWUbihU_Yia Ubm Zcfa qžZfca iXYi]VYfUhYiW\YUh|b[ihciUVW]XYbhU`mWcdm]b[iZfca iUigci fWik]h\ci hiUW_bck iYX[Ya Ybh'i

IBGK '[fci dg'd'U[]Uf]ga ']bhc'h\Y'Zc``ck]b['WUhY[cf]Yg.

7 cdm]b[.'i g]b['h\Y'gUa Y'cf'j Yfmg]a]`Uf'k cfXg'hc'h\Y'cf][]bU`hYl h'cf']XYU'k]h\ci h'UW_bck `YX[]b['h\Y gci fW'cf'i g]b['ei chUh]cb'a Uf_g"'H\]g'U`gc'Udd`]Yg'hc']a U[Ygž'Ufh'UbX'XYg][b'dfcYWhgž'Ug'k Y``'Ug dfYgYbhUh]cbg'k\YfY'gca YcbY'dfYgYbhg'Ubch\Yf'g']XYUg'cf'k cfXg'k]h\ci h'WfYX]h'

⇒ Uddfcdf]UhY 'dUfUd\fUg]b[...7\Ub[]b['U'ZYk 'k cfXg'UbX'd\fUgYg'k \]'Y 'a cghmfYhJ]b]b['h\Y'cf][]bU` ghfi Wh fY 'UbX#cf'dfc[fYgg]cb'cZ]XYUg'cZh\Y'cf][]bU'žUbX']bZcfa Uh]cb'k]h\ci hUW_bck `YX[Ya Ybh'H\]g'U`gc Udd`]Yg']b'dfYgYbhUh]cbg'k \YfY'gca YcbY'dUfUd\fUgYg'Ubch\Yf'g']XYUg'cf'k cfXg'k]h\ci hWfYX]hUbX'hc d]YW]b['hc[Yh\Yf'ei chYg'UbX'dUfUd\fUgYg']bhc'U'bYk 'k \c`Yžk]h\ci hUddfcdf]UhY'fYZYfYbW]b["

7 c``i g]cb. 'k cf_]b['k]th 'cth Yfg'Vi hidUgg]b['cZZth Y 'k cf_'Ug'U'dYfgcb'g']bX]j]Xi U``k cf_"'7 c``i g]cb'U`gc]bWi XYg'dfcj]X]b['mci f'k cf_'thc'Ubcth Yf'ghi XYbh'VYZcfY'th Y'Xi Y'XUlfYZcf'Zcf'th Y'di fdcgY'cZth Ya

- i bXYfgfUbX mci f'f][\hg'UbX'fYgdcbg]V]`]hJYg'Ug'U'gh XYbhUhl BGK
- VY`Uk UfY`cZd`U[]Uf]ga ž`Wcdmf][\hzil BGK `Gh XYbh7cXY`cZ7cbXi WhUbX`5VWWdhUv`Y`I gY`cZ I BGK `=\forall H`F Ygci f\W\g`Dc`]\wh
- VY 'Uk UfY 'cZh\Y 'ghUbXUfXg 'cZVY\Uj]ci f'Yl dYWYX 'cZYj YfmcbY ']b 'h\Y 'l BGK 'Wca a i b]hm
- `cWUHY 'gYfj]WYg'UbX ']bZcfa UH]cb'UVci hI BGK 'UbX'I BGK '@]VfUfm

Gca Y'cZh\YgY'UfYUg'k]``VY'ZJa]`]Uf'hc'mci ž'ch\Yfg'k]``VY'bYk"'; U]b]b['U'gc`]X'i bXYfgHJbX]b['cZU``h\YfY`UhYX'UgdYWng'cZ9@+69'k]``\Y`d'mci 'a U_Y'h\Y'a cghicZmci f'ghi X]Yg'UhI BGK "'\\hd.##qi VYWfi |XYg"`]VfUfm'i bqk "YXi "Ui #\`]qY#JVci hY`]qY

5 WUXYa]W = b Zcfa Uh cb.

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- fYei Yghg Zcf Yl hYbg]cb/
- `UhY`gi Va]gg]cbg`[i]XY`]bYg/
- fYj]Yk 'cZa Uf_g/
- I BGK '< YU`h\ 'UbX'GUZYhm'dc`]W[Yg/
- YI Ua]bUhcb dfcWXi fYg/
- gdYWJU``Wcbg]XYfUhJcb`]b`h\Y`Yj YbhcZ]``bYgg`cf`a]gUXj Ybh fY/
- gh XYbhYei]lmUbX X]gUV]`]lm/
- UbX'ch\Yf'YggYbhJU`'UWUXYa]W]bZcfa UhJcbž'gYY

\hdg.#k k k "Uffg"i bgk "YXi "Ui #W ffYbhgh XYbhg#UWJXYa]W]bZcfa Uf]cb#dfchcWc`g![i]XY`]bYg#

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7 F = 7 C G 'Dfcj]XYf'7 cXY. '\$\$\$-,;