

# **ARTS2698**

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j Uf]ci g`gcW]U`ždc`]h]WU`žUbX`fY`][ ]ci g`WcbhYl hgž]bhfU!W``hi fU``mUbX`]bhYfW``hi fU``m'\Mci 'k ]```Yl Ua ]bY`]ggi Yg
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: YYXVUW\_`]b`k f]h]b[ 'Zfca 'h\Y``YWh fYf`UbX`cfU``miZfca 'h\Y`WUgg`UbX'h\Y``YWh fYf"

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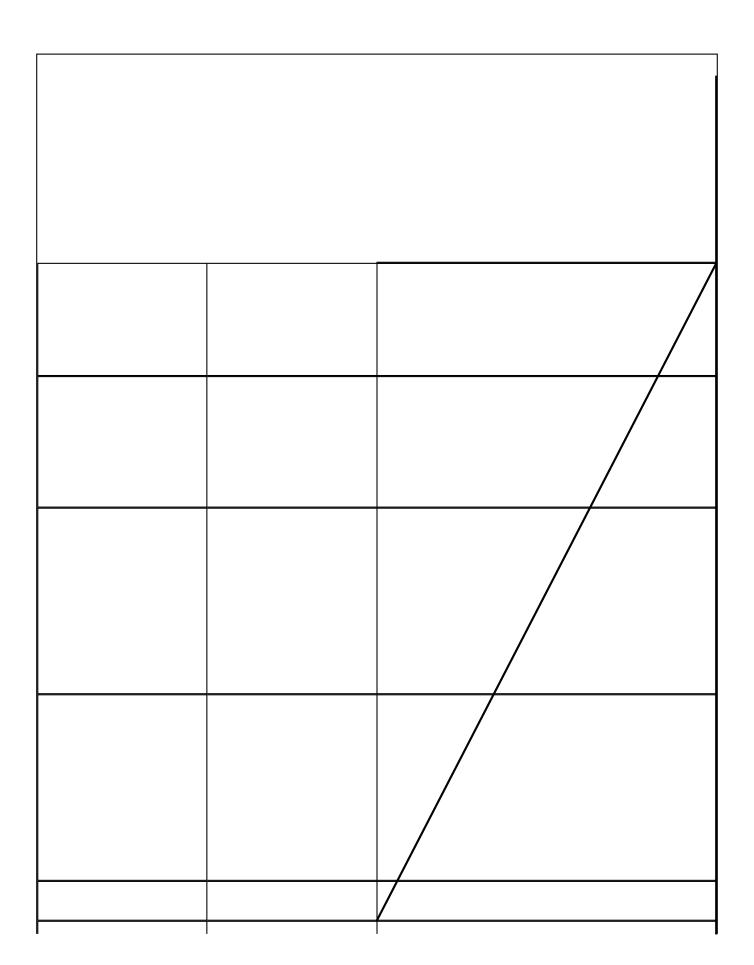
- 5 HhY b X U b W 'c Z @Y W f Yg#H i hcf] U 'g '] g 'a U b X U hcfm] b 'h \] g 'W c i fgY " I b Y I W g Y X 'U V g Y b W 'Z f ca 'a cfY h \ U b '&\$ i 'c Z @Y W f Yg#H i hcf] U 'g 'k ] ``f Y g i `h ] b 'h Y 'U k U f X 'U 'Z U ] ``[ f U X Y " ' '
- D'YUgY'W egdWfZSfkage[Y`cb'h\Y'kYY\_`m'UhYbXUbW'``]gh''
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