

MDIA1004

BYkg: i bXUa YbHJ`g

HYfa "Hk c" ## "&\$&\$

7ci fgY'Cj Yfj]Yk

GHJZZ7cbHJWh8YHJ]`g

7cbj Ybcfg

B Ua Y	9a U]`	5j U]`UV]`]lm	@cWJhjcb	D\cbY
8 f [:] ? Yff]Y [:] 8 Uj]Yg	_"XUj]Yg4 i bgk "YXi "Ui	,	FcVYfh KYVghYf" %%7	

Hi hcfg

B Ua Y	9a U]`	5j U]`UV]`] m	@cWUhjcb	D\cbY
>c\b′6i fZ th]b WUgg ! d YUgY gYY Wobj Ybof ? Yff]Y 8 Uj]Yg Zof Uddo]bha Ybhg ci hg]XY WUgg h]a Y	j]U'Ya U]`	

GWXcc~7cbHJWh~abZcfa Uh]cb

GWXcc``cZh\Y`5fhq'UbX'AYX]U

Fcca " %&ž@Yj Y`" žFcVYfhK YVghYf'6i]`X]b[ff %(Ł

D\cbY. 'f\$&Ł'-',) '(,) *

9a U]`. 'gUa 4 i bgk "YXi "Ui

K YVq]hY. k k k "Ufhq"i bak "YXi "Ui #qUa

 $\label{eq:hamiltonian} $$HY'GWCC``cZhY'5ftg'UbX'AYX]U'kci`X``]_Y'tc'FYgdYWM\cong \cong m5W_bck`YX[Y'h\Y'HfUX]tjcbU``7igtcX]Ubg\cong h\Y'6YXY[U'`fPYbg]b[hcb'WJadig\cong ix', UX][U'`fP]hmUbX'5fti/'8Yg][b'7UadigYg\cong iybUx'h\Y'B[ibbUkU`dYcd'Y'fbighfU`]Ub'8YZYbW': cf\w'5\\\XYam]b'7Ub\YffU\cozh\Y'`UbXg'k\YfY'YUW\\WJadig'cZIBGK']g`c\\Ully\X''$

5ggYgga Ybh

H\Y'YI Ua 'k]``VY'H_Y'\ca Y'cdYb'Vcc_"'Mci 'k]``\Uj Y'&('\ci fq'hc'Wca d'YhY']h'

Hi hcf]U`g`UfY`Wca di `gcfm''C b`mik c`WUb`VY`a]ggYX"`D`YUgY`gYY`h\Y`Wcbj Ybcf`cf`mci f`h hcf`]Zmci `UfY i bgi fY"`GdYW]U``Wcbg]XYfUh]cb`fYei]fYX`]b`WUgYg`cZa cfY`h\Ub`k c`UVgYbWkg"`D`YUgY`bchY`h\YmUfY`&")\ci fg`UbX`k]```VY`cb`]bY"`5\WWfgg`j]U`7c``UVcfUhY``]b_g`cb`A ccX`Y"

GdYW]U`Wcbg]XYfUh]cb'j]U'a mi bgk "YXi "Ui ']g'fYei]fYX`Zcf'Ubm`UhY`UggYgga Ybhgžch\Yfk]gY`]h']g') I 'dYf'XUm''D`U[]Uf]ga 'k]``VY`fYZYffYX'hc'h\Y`GW\cc`fg'Yh\]Wg'cZZ]WYf"

7 cbgi `h]b['\ci fg'k]``'VY'Uj U]`UV`Y'ci hg]XY'hi hcf]U`'h]a Yg'! Z- ZYf]XYc_X'U]a Y4 mi bgk "YXi "Ui 'Zcf`'h]a Y

5ggYgga Ybh& BYk g dfcXi Wh]cb dUW_U[Y

GhUfhXUhY. Bch5dd`]WUV`Y

@Yb[h\.**\$\$!'+\$\$"k cfXg"cf"Zci f"hc"Z|j Y"a]bi hY"Ui X]c

8YHJ]`g.

 $Cf][\]bU``bYk\ g`dfcXi\ Wf]cb'dUW_U[\ Y\check{z}'*\$\$`-'+\$\$`k\ cfXg`gi\ Va\]hhYX`CF'Zci\ f`hc'Z]j\ Y!a\]bi\ hY`fUX]c'bYk\ g\ dUW_U[\ Y'j\]U`A\ ccX`Y''$

; fUXYX'j]U'UggYgga Ybh'Wf]hYf]Už'k f]hhYb'ZYYXVUW_j]U'@A G"

5XX]h]cbU`XYhU]`g.

Hcd]WUgg][bYX]b WUgg"

Cf][]bU`d\chcfYei]fYX"

A]b]a i a ˈkk c ˈ]bhYfj]Yk gžd`i g Yj]XYbW cZgi dd`Ya YbhUfmfYgYUfW."

B UffUhjj Y cf 'hfUX]hjcbU`bYk g 'ghmY' 'ci fbU`]ga "

Gi Va]gg]cb bchYg.Gi Va]gg]cb j]U A ccXY

5ggYgga Ybh' . CdYb 6cc_ HU_Y <ca Y 9l Ua

GhUfh'XUhY. H65

8YHJ]`g.

H\Y'YI Ua 'k]``'VY'U'HU_Y'\ca Y'cdYb'Vcc_'YI Ua 'H\Uhk]``']bj c`j Y'dfUWfJWY'VUgYX'k f]hJb['HJg_gž'Udd`]YX _bck `YX[Y'UbX'fYgYUfW\"'GdY\JZJW]bZcfa UhJcb'hc'VY'[]j Yb']b'WUgg"

H\Y`YI Ua `k]```VY`gW\YXi `YX`]b`K YY_`%%"`5`&(`\cif`fja Y`dYf]cX`k]```VY`[]j Yb`fc`Wca d`YfY`f\\Y`YI Ua "`

5XX]h]cbU`XYhU]`g.

91 Ua "XUhY"Hc"6Y"5Xj]gYX"

 $\label{thm:condition} \mbox{Hi fb]h]b$ "gYh]b$ [. "H\]g$ "Ugg][ba Ybh]g$ "gi Va]hhYX"h\fci [\ "Hi fb]h]b$ "UbX"ghi XYbhg"Xc"bchgYY"Hi fb]h]b$ g]a]`Uf]hmfYdcfhg"$

5 hm/b XUb VW F Yei]fYa Ybhg

Ghi XYbhgʻa i ghiUhhYbXʻ, \$`i 'cZhi hcf]Uʻgʻhcʻa YYhiUhhYbXUbWYʻfYei]fYa YbhgʻcZh\]gʻWci fgY"

7ci fgY GWX YXi `Y

J]Yk 'WUgg'hja YhUV'Y

H]a YHJV`Y

8 UhY	HmdY	7 cbhYbh
K YY_'%'%'>i bY'!') '>i bY	@YWi fY	±olfcXi WhjcbinchNYWcifgY" ;`fWcSUf[hW>WUfgdWa`f`Wh[S5a^STacSfW,dWWdfa ?aaV~Wfa \a[fZW^`]ž @YWhifYg'k]``VY`]jYž]bhYfUWhjYžUbXigcaYhjaYg \UjY'kf]h]b['YIYfW]gYg"'Mcifi`VY`]bj]hYX'ncig\UfY
	HTbcf]b`rial	bYk g``]b_gž'Ug_'ei Ygh]cbg'UbX'Wca a Ybh' 3 ^^fgfad[S^e i [^TWdg` h[S 5 a ^STadSfWz <a[kagd<br="">fgfad[S^h[S 5 a ^STadSfWz 6 a ` af ei Sb kagdfgfad[S^e Sdag` V Žkag i [^TW_ Sd] WW STeW fz</a[>
K YY_'&.', '>i bY'!'%& >i bY	@YVVi fY	@YWi fY W.Ub[Y'h\]g k YY_cb`mhc HI 9G85M %\$Ua Xi Y'hc E i YYbfig 6]fh\XUmdi V`]W\c`]XUm' C dh]cbU`UhhYbXUbW. BYk g k f]h]b[. fYj]g]cb cZ IfUX]h]cbU`bYk g ghmY UbX]bhYfj]Yk]b['%\$%" <a[]="" fzw="" fzw5a^stacsfw1="" s^"<="" td="" wufgdwh[s=""></a[>

K YY_" ."%) ">i bY"! "%- >i bY	@YWhi fY	Cb`]bY'@YWifY.'BUffUh]jY'bYkg' <a[a`?aav^w<="" h[sfzw5a^stacsfw^]="" th=""></a[>
		FYUX]b[g FYZYf'hc'AccX'Y
	Hi hcf]U`	BUffUhjj Y'bYk g'k f]hjb['dfUWjWY"
		<a[]a`?aav1\t<="" kagdfgfad(s^h[s5a^stadsfw1="" th=""></a[>
K_YY(.^&&^>i bY^!^&* >i bY	@YWhi fY	Cb`]bY``YWhifY.''H\Y'ibhc`X'ghcfm'FYgYUfW\]b[''
>I DY		6f]YZZcfcf][]bU`glcfmdfcXiWh]cb'dUW_U[Y
		<a[5=""]="" ^[="" ^sta="" ^wz<="" a="" a`?="" dsfw="" h[s="" td="" v=""></a[>
		FYUX]b[g
		FYZYf'hc'AccX`Y
	Hi lcf]U`	Cf][]bU`glcfmfYgYUfW\`UbX`VfU]bglcfa]b["
		<a[`h[s5a^stacsfwa`?aav↑vz< td=""></a[`h[s5a^stacsfwa`?aav↑vz<>
K YY_').'&-'>i bY'!'' '>i `m	@YWn fY	Cb`]bY'@YWnifY.'+bhfcXiWn]cb'hc'bYkg'fUX]ckf]h]b['UbX']bhYfj]Yk]b['Wihg
		<a[td="" wufgdwh[s5a^stadsfw1[]a`?aav1\dz<=""></a[>
		FYUX]b[g
		FYZYf'hc'AccX'Y"
	Hi hcf]U`	Cf][]bU`ghcfm]XYU'd]hWX 'ZYYXVUW_
		<a[]="" a`?aav^w<="" kagdfgfads^h[sfzw5a^stadsfw1="" td=""></a[>
		DWeWSdJZ 3eeWee_Wf6gWz
K YY_'*.'*'>i `m!''\\$'>i `m	FYUX]b[The state of the s
K YY_`+.`% `>i `mi!`%+`>i `m		Cb`]bY``YWhifY.']bhYfj]Yk]b['UbX'cd]b]cb'hfUdg'
		<a[]="" a`<br="" kagdfgfad(s^h[sfzw5a^stadsfw1="">? aaV^WZ</a[>
		FYUX]b[g
		FYZYf'hc'AccX`Y"
1	1	

FYgci fWyg

DfYgWf]VYX F Ygci fWYg

FYWca a YbXYX HYI hVcc "

 $5b^{\circ}9Vcc_g\ci^{X'}VY^{\circ}UjU]^{\circ}UV^{\circ}Y^{\circ}hc^{\circ}Vcffck^{\circ}j^{\circ}U^{\circ}UBGK^{\circ}]VfUfm''^{\circ}K^{\circ}Y^{\circ}Xc^{\circ}bchYldYWhmci^{\circ}hc^{\circ}Vimh^{\circ}]g^{\circ}hYlh^{\vee}cc_'']c^{\circ}VfZ^{\circ}Z^{\circ}mci^{\circ}k^{\circ}C^{\circ}Q^{\circ}Cd''$

Hfi 'j``cžH'f&\$% Ł"I dff YS`VDWbadf Y@W'e Kag 5S` GeW'Clcb". Fci hYX[Y"

⊋mci 'UfY'dfcXi Wjb['Ui X]cž5I 857 ±IM']g'U'ZfYY'cb`]bY'Ui X]c'YX]hjb['gcZhk UfY'cf'h\Y'a cfY'UXj UbWX 5I 8±I±€B']g'U'WYgg]V'Y'j]U'58C69'7 fYUhjj Y'7 'ci X'''

FYWca a YbXYX FYgci fWyg

H\Y`Wci fgY`fYei]fYg`Vch\`bUhJcbU``UbX`]bhYfbUhJcbU``W ffYbh`UZU]fg`_bck `YX[Y`k \]W\`i gi U``m`]bZcfa g`h\Y YI Ua "'=i]g`fYWca a YbXYX`ghi XYbhg`fYUX`k]XY`mUWfcgg`5i ghfU`]Ub`UbX`]bhYfbUhJcbU``bYk g`UbX`W ffYbh UZU]fg`d`UhZcfa g"

Gi [[YghYX ZfYY bYk g g]hYg.

567]j Yk 'bYk g'W.UbbY`.'+"' \$'fYdcfh'UbX'Yj Yb]b['bYk g
UVWbYh'Ui 'Zcf'cb`]bY'bYk g"
567 F UX]c 'B UhJcbU`'#Hf]d`Y'>#567 'GmXbYmF UX]c
H\Y'Dfc'YWh'BYhk cf_'%\$'
gVg"Wca "Ui '#bYk g
F ZW9 gSdV[S` 'h\Y[i UfX]Ub"Wca #Ui
I G'Dc`]hJWg'H\Y'@UhY'G\ck 'k]h\'GhYd\Yb'7c`VYfhfJ]U'Nci Hi VYŁ/Wbb"Wca /@UhY'B][\hik]h\'GYh\'A YmYfg
fJ]U'Nci Hi VYŁ/>c\b'C`]j Yf'

@]a]hYX ZfYY i]Yk]b['! 'Uj U] `UV `Y i]U I BGK '`]VfUfm'

FZWEKV`WK?ad[Y:WcsV'ga\"Wca"Ui FZW@Wi Kad|F[We'bmha Yq"Wca

9b[`]q\``Ub[i U[Y'<cb[?'cb[`'UbX'7\]bU. FZWEaqfZ 5Z[S ? ad [Y Baef qWa d"Wca

.

7 ci fgY 9j U'i Uhcb UbX 8Yj Y'cda Ybh

: YYXVUW_'h\fci [\ci hh\Y'Wci fgY']g'k Y`Wca Y'Ug'k Y``'Ug']b'fa m'YI dYf]YbWffigi fj Ymg'''K Y'YbWci fU[Y'mci hc 'Yhi g'_bck 'mci 'UfY'ghfi [[']b['cf'YI dYf]YbW]b['X]ZZ]W 'h]Yg'k]h\'cb`]bY'h hcf]U'g'Uhh\Y'h]a YžfUh\Yf'h\Ub k U]h]b['i bh]'h\Y'bX'cZh\Y'Wci fgY'''

H\Y`Wci fgY`\Ug`Yj c`j YX`Zfca `hfUX]hjcbU``bYk g`fYdcfhjb['hc`]bWi XY`h\Y`bYk 'a YX]U`YI dYWUhjcbg`cZ bUffUhjj Y`bYk gžgcWjU``a YX]U`fYdcfhjb[ža cV]`Y``ci fbU`]ga `UbX`\Ug`U`[fYUhYf`ZcW g`cb`fUX]c`k f]hjb["`H\]g $mYUf'k\ Y'UfY'UXUdh]b[\ 'fh\ Y'Y|\ Ua\ 'Zcf'cb`]bY'UbX'U'gc'cZZYf]b[\ 'fh\ Y'cddcfhi\ b]hmhc'dfcXi\ WY'Ui\ X]c'Ug'mci\ fa \ U'cf'Ugg][\ ba\ Ybh'$

 $5g`A 8 = 5\%$$\& ZcW gYg`cb`HfUX]HjcbU``bYk g`k f]Hjb[``g_]``gž'H\]g`g_]```]g`cb`mVf]YZmWcj YfYX`]b`H\]g`Wci fgY''`HcUgg]ghghi XYbhg`k \c`\Uj Y`bchdfYj]ci g`mghi X]YX`bYk g`k f]Hjb[`žk Y`YbWci fU[`Y`mci `hc`UWW`gg`fYj]g]cb fYgci fW'g`cb`A ccX`Y`UbX`hc`a U_Y`Ub`Uddc]'Y` bX`h ``Wci fg``W Uj j Y Y \U WY hi ']Y$

Gi Va]gg]cb cZ5ggYgga YbhHUg_g Hi fb]h]b Gi Va]gg]cb

5 WUXYa]W<cbYghmUbX D`U[]Uf]ga

D`U[]Uf]ga `]g`i g]b['h\Y`k cfXg`cf`]XYUg`cZch\Yfg`UbX`dfYgYbh]b['h\Ya `Ug`mci f`ck b"`±hWJb`hU_Y`a Ubm Zcfa gžZfca `XY`]VYfUhY`W\YUh]b['hc`UWW]XYbhJ``mWcdm]b['Zfca `U`gci fWY`k]h\ci hUW_bck `YX[Ya Ybh'

IBGK [fcidg'd'U[]Uf]ga]bhc'h\Y'Zc``ck]b['WUhY[cf]Yg.

 $7 \text{ cdm}b[...i g]b[...h\Y.gUa Y.cf.j Yfmig]a] \Uf'k cfXg'hc'h\Y.cf][]bU''hYl h'cf']XYU'k]h\ci h'U\V_bck `YX[]b[...h\Y.cf][]bU''hYl h'cf']XYU'k]h'cf']$



5 WUXYa]W = b Zcfa Uh cb

: cf'YggYbhJU`'gh XYbh']bZcfa UhJcb'fY`UhJb['hc.

- fYei Yghg 'Zcf'Yl hYbg]cb/
- `UhY`gi Va]gg]cbg`[i]XY`]bYg/
- fYi]Yk 'cZa Uf_g/
- I BGK '< YU`h\ 'UbX'GUZYhm'dc`]W[Yg/
- YI Ua]bUh]cb dfcWYXi fYg/
- gdYWJU`Wcbg]XYfUHjcb`]b`H\Y`Yj YbhcZ]``bYgg`cf`a]gUXj Ybh fY/
- qh XYbhYei]miUbX X]qUV]`]m/
- UbX'ch\Yf'YggYbhJU`UWUXYa]W]bZcfa UhJcbžgYY

\hdg.#k k k "Ufhg"i bgk "YXi "Ui #W ffYbhgh XYbhg#UWJXYa]W]bZcfa Uh]cb#dfchcWc`g![i]XY`]bYg#

.

⇒a U[Y'7fYX]h

BY[UhjjY'GdUW'j]U'DYIY`'7fYUhjjY'7ca a cbg'`]WYbWY"

7F = 7CG

7F = 7CG Dfc|]XYf 7cXY. \$\$\$-,;

5W_bck `YX[Ya YbhcZ7ci bhfm

 $K Y : UW\underline{b} ck `YX[Y : h, Y : 6YXY[U : dY cd `Y : k \ c : UfY : h, Y : hfUX]h\underline{b} cb : `W ghcX]Ubg : cZh, Y ``UbXg : cb : k \]WX : I B G K ? Ybg]b[hcb : WUa di g :]g ``cWUhYX''$