

MDIA2003

A YX]U 7 cbhYbh 7 fYUh]cb

7ci fgY^{*}Cj Yfj]Yk

GHJZZ:7cbHJWh:8YHJ]`g

7cbj Ybcfg

B Ua Y	9a U]`	5j U]`UV]`] m	@cWUhjcb	D\cbY
DYHYFK\]HY	·	K YX'&"\$\$'da '!'' "\$\$ da 'fb'YUgY'Ya U]`'hc UffUb[Y'Ub Uddc]bha YbhŁ	0,	L)&'*(

GWXcc`7cbHJWh ≠bZcfa Uh]cb

GWLcc``cZhLY`5fhg`UbX`AYX]U

Fcca " ‰ž@Yj Y`" žFcVYfhK YVghYf'6i]`X]b[fJ %(Ł

D\cbY.`f\$&Ł'-',)`(,)*

9a U]`. '

7ci fgY'8YW]`g

7 fYX]hDc]bhg**

Gi a a UfmcZh\Y 7ci fgY

H\]g`Wci fgY`]g`WcbWffbYX`k]h\`h\Y`g_]`g`fYei]fYX`hc`dfcXi WY`UbX`Wf]h]WU``mUbU``mgY`h\Y``cb[Yfža cfY`]b! XYdh\`Zcfa g`cZ'ci fbU`]ga `_bck b`Vmgi W\``UVY`g`Ug`"ZYUhi fY"`UbX`"XcW a YbhUfm"''`H\Y`Wci fgY`k]```ZcW g`cb h\YgY``cb[Yf`Zcfa g`Ug`h\YmcdYfUhY`]b`bYk gdUdYfgža U[Un]bYgžfUX]c`UbX`cb`]bYž`UbX`\ck `h\Ymj Ufm UVWcfX]b[`hc`gi V'YVMa UhHYf'-']"Y''`UWWcfX]b[`hc`k \Yh\Yf`h\YmUfY`WcbWfbYX`k]h\`W`ffYbh`UZU]fg`UbX`gcW]U`]ggi Ygžcf`k]h\`Ufhg`UbX`YbhYfhU]ba Ybhcf``]ZYghmY`UbX``Y]gi fY`hcd]Wg"`H\Y`Wci fgY`k]```U`gc`dfcj]XY ghi XYbhg`k]h\`Ub`i bXYfghUbX]b[`cZk\Uhi]g`hmd]WU``m]bj c`j YX`]b`h\Y`dfYdUfUh]cb`cZZYUhi fYg`UbX XcW a YbhUf]Yg`-Y"["'\ck 'h\YmUfY`WcbWf]j YXž`\ck 'h\Yma UmfYei]fY`h\Y`W`h]j Uh]cb`cZUddfcdf]UhY "WcbhUWg"žUbX`h\Y`hmdYg`cZfYgYUfW\`UbX`]bhYfj]Yk]b[`i gi U``mYa d`cmYX"`+b`h\Y`dfcWgg`cZXYj Y`cd]b[

5ggYgga Ybh

5ggYgga Ybh HUg_g

5ggYgga Ybh'HJg_	K Y][\h	8i Y'8UHY	Gh XYbh@YUfb]b[Ci hWca Ygʻ5ggYggYX
Dcfh7c`]c'fj Uf]ci g'a YX]UŁ'	&\$I	Bch5dd`]WUV`Y	%ž'&ž'' ž'(
A YX]U WebhybhdfydUfUhjeb UbX dfcXi Whjeb HUg_'%	')।	Bch5dd`]WUV`Y	%ž'&ž'' ž'(
A YX]U Wcbh/bhdf/dUfUhjcb UbX dfcXi Wjcb HJg_ &	()।	Bch5dd`]WUV`Y	%ž'&ž'' ž'(

5ggYgga Ybh'8YhJ]`g

5ggYgga Ybh% DcfhZc`]c fJ Uf]ci g a YX]UŁ

Bch5dcch5thchUhY.Bch5dd`]WUV`Y

8YHJ]`g.

₽X]jj]}XiW`

%\$\$"k cfXg"Yei]j U`Ybh

: YYXVUW_'j]U'@A G

5XX]h]cbU``XYhU]`g.

 $\label{eq:higher_high_substitution} \mbox{Hi fb]h]b"gYhh]b[."H\]g"]g"bchU"Hi fb]h]b"Ugg][\ ba\ Ybh$

 $5\,ggYgga\ Ybh\&\ A\ YX]U\ WcbhYbhdfYdUfUh]cb\ UbX\ dfcXi\ Wh]cb\ hUg_\ \%$

Hi fb]h]b 'gYh]b[. 'H\]g ']g 'bchU'Hi fb]h]b 'Ugg][ba Ybh

5ggYgga Ybh' . A YX]U WcbhYbhdfYdUfUh]cb UbX dfcXi Wh]cb HJg_ &

GHJfhXUhY. Bch5dd`]WUV`Y

8YHJ]`g.

₽X]j]Xi U`

% \$\$"k cfXg"Yei]j U`Ybh

: YYXVUW_'j]U'@A G

H\]g`]g`h\Y`ZbU``UggYgga a Ybh

.

5XX]h]cbU``XYhJ]`g.

GYY'Wci fgY'A ccX`Y'g]hY'Zcf'XYhU]`g"

Hi fb]h]b gYh]b[. H\]g]g bchU Hi fb]h]b Ugg][ba Ybh

5 http://bxubww.FYei]fYaYbhg

 $5\,\text{thY}bXUbWY^*]g^*fYei~]fYX^*UhVch\ ``YWh~fYg^*UbX^*h~hcf]U^*g^*fJ~\$^*dYfWYbh^*UhYbXUbWY^*a~]b]a~i~a~Ł"$

7ci fgY GWX YXi `Y

J]Yk~WU % dYfWybhUttybXUbWy~a]b]aiaŁ"

	1

		&"`I dXUhY`cb`W`ffYbh]ggi Yg`]b`a YX]U`Wcj YfU[Y
	Hi kcf]U`	fGYY`A ccX`Y`k YVg]hY`Zcfi dXUhYX`]bZcfa Uh]cb UVci hh\Y`hi hcf]U``!`gW\YXi `Y`a UmW\Ub[Y`Ug W`ffYbhbYk g`Yj Ybhg`i bZc`X"Ł
		DfcZjYkf]hjb['h/ghfi b'!'df]bhghcfmUbXg\cfhUi X]cdUw_U[Yf('a]bi h/gk'dfYdUfYX]b'UXjUbW'cZhi hcf]U`Zfca fYWcfX]b[g#fUbgWf]dhg'cZ]bh/fj]Ykg
K YY_'(.', 'A UfVX'!'%& A UfVX	@YWhi fY	%":>ci fbU`]gh]W±pgd]fUh]cb.:"ZYg\ž:W ffYbhUbX Yb[U[]b["'!''h\Y']XYbh]Z]WUh]cb'f&f'W&bWdh]cbEcZ di V`]g\UV`Y'X][]hU`'W&bhYbh
		&"'A UbU[]b['cb`]bY'di V`]WUh]cbg''!'7 cbhYbh A UbU[Ya YbhGmghYa g'f7 A GŁ#k YV'dU[Y'XYg][b
	Hi hcf]U`	fGYY'A ccX`Y'k YVg]hY'Zcf'i dXUhYX']bZcfa Uh]cb UVci hh\Y'hi hcf]U`'!'gW\YXi `Y'a UmW\Ub[Y'Ug W'ffYbhbYk g'Yj Ybhg'i bZc`X"Ł
		±blYfj]Yk 'k cf_g\cd'dfYdUfUljcb'! 'Y"["'Yl d`cfY dchYbljU```]bYg'cZ]bei]fmž'dchYbljU`'″diV`]g\UV]`]lm″/ XfUZrigcaY'eiYgljcbg
K YY_^).^%)^A UfWX^!^% A UfWX	@YWhi fY	Dcgg]V`m'±bHYfj]Yk]b['K cf_g\cd'fXYdYbX]b['cb'\ck h\Y'gW\YXi `Y'dUbg'ci Hz
	Hi hcf]U`	%"FYj]Yk 'cZghcfm']XYUg'gi Va]hhYX'Zcf'hihY'dfYd'
		&"`7 Ubj Ugg]b[`cZdfca]g]b[`hcd]WUfYUg`Zcf]ggi Yg#fYbX`ZYUh fYg
K YY_'*.'&&'A UfW\'!'&* A UfW\		: `YI`kYY_'!`'bc``YWn fY'cf'h hcf]U`
		: `YI 'k YY_!'bc'hi hcf]U`g
K YY_'+.'&-'A UfVX'!'& 5df]`	@YWhifY	=ggi Yg#fYbX`ZYUhi fYg`—`]XYUgž`Ub[`Ygž`ghm`Yg`UbX ghfi Whi fYg
	Hi kcf]U`	GYY'Wci fgY'A ccX`Y'g]hY'Zcf`XYhJ]`g"
K YY_', .') '5df]`'!'- '5df]`	@YWhifY	Jc*

K_YY_'%\$."%="5df]`'!"&' 5df]`	@YWhi fY	H65
		fl]bU``Ugg][ba YbhX]gW gg]cbžgi [[Ygh]cbg`YhWŁ GYY`Wci fgY`A ccX`Y`g]hY`Zcf`XYhJ]`g"

Fygci fWyg

DfYgWf]VYX F Ygci fWYg

Gi Va]gg]cb cZ5ggYgga YbhHUg_g

Hi fb]h]b Gi Va]gg]cb

Image: Ybwei bhyfu'dfcv'ya k \yb'uhhya dhjb['hc'gi va]hmci f'Ugg][ba Ybhh\fci [\ 'Hi fb]h]bz'd'YUgY

Hy'Yd\cby'9| hy'fbu''Gi ddcfhcb'-',) '' ' ' %cf'Ya U]''h\Ya 'cb'Y! hy'fbu'hy'hgi ddcfh4 i bgk "YXi "Ui "''Gi ddcfh
\ci fg'UfY', .\$\$Ua '-'%\$.\$\$da 'cb'k YY_XUmg'UbX'-.\$\$Ua '-').\$\$da 'cb'k YY_YbXg'fl *) 'XUmg'U'mYUft"'=Z'mci
UfY'i bUV'Y'hc'gi va]hmci f'Ugg][ba YbhXi Y'hc'U'ZJi 'hk]h\ 'Hi fb]h]b'mci 'a Um'Udd'mZcf'Ub'Y! hy'bg]cbz'Vi hmci
a i ghfYhJ]b'mci f'h]W_Yhbi a VYf'Zfca '9! hy'fbu''Gi ddcfhfU'cb['k]h\ 'Ubmch\Yf'fy'Yj UbhXcW a Ybhgt'hc
]bWi XY'Ug'Yj]XYbW' 'hc'gi ddcfhmci f'Y! hy'bg]cb'Udd']WUh]cb"'=Zmci 'Ya U]''9! hy'fbu''Gi ddcfhmci 'k]'`
Ui hca Uh]WJ'`mfYW']j Y'U'h]W_Yhbi a VYfz'Vi h]Zmci 'hY'Yd\cbY'mci 'k]``bYYX'hc'gdYW]Z]WJ'`mUg_'Zcf'cbY''
Hi fb]h]b'U'gc'dfcj]XYg'i dXUhy'g'cb'h\Y]f'gmghYa 'ghUh' g'cb'Hk]hyf''

; YbYfU`mž'UggYgga YbhiHug_g'a i ghVY'gi Va]hhYX'Y`YVWfcb]\WJ``mij]U'Y]h\Yf'Hi fb]h]b'cf'U'A ccX`Y Ugg][ba Ybh''=b']bgHJb\W'g'k \YfY'h\]g']g'bchdcgg]V`Yž']hk]```VY'gHJhYX'cb'mci f'\\circ i fgY'g'A ccX`Y'g]hY'k]h\U`hYfbUh]j Y'gi Va]gg]cb'XYHJ]`g"

cfi]bZcfa Uhjcbicbi\ckihcigi Va]hUgg][ba Ybhgicbi]bYij]UiA ccXiY.i\hdg.#gh XYbhi bgk "YXi "Ui #\ck! gi Va]hUgg][ba Ybha ccXiY

5 WUXYa]W<cbYghmUbX D`U[]Uf]ga

D`U[]Uf]ga `]g`i g]b['h\Y`k cfXg`cf`]XYUg`cZch\Yfg`UbX`dfYgYbh]b['h\Ya `Ug`mci f`ck b"`±hWJb`hU_Y`a Ubm Zcfa gžZfca `XY`]VYfUhY`W\YUh]b['hc`UWW]XYbhJ``mWcdm]b['Zfca `U`gci fWY`k]h\ci hUW_bck `YX[Ya Ybh'

IBGK [fcidg'd'U[]Uf]ga]bhc'h\Y'Zc``ck]b['WUhY[cf]Yg.

 $7 \text{ cdm}b[...i g]b[...h\Y.gUa Y.cf.j Yfmig]a] \Uf'k cfXg'hc'h\Y.cf][]bU''hYl h'cf']XYU'k]h\ci h'U\V_bck `YX[]b[...h\Y.cf][]bU''hYl h'cf']XYU'k]h'cf']$

- i bXYfgHUbX'mci f'f][\hg'UbX'fYgdcbg]V]`]h]Yg'Ug'U'gh XYbhUhI BGK
 VY'Uk UfY'cZd`U[]Uf]ga ž'Wcdmf][\hz'I BGK 'Gh XYbh7cXY'cZ7cbXi WhUbX'5VWWdhUV`Y'I gY'cZ IBGK =7 HF Ygci fWrg Dc`]Wh

5 WUXYa]W = b Zcfa Uh cb

: cf'YggYbhJU`'gh XYbh']bZcfa UhJcb'fY`UhJb['hc.

- fYei Yghg 'Zcf'Yl hYbg]cb/
- `UhY`gi Va]gg]cbg`[i]XY`]bYg/
- fYi]Yk 'cZa Uf_g/
- I BGK '< YU'h\ 'UbX'GUZYhm'dc`]\\\Yg/
- YI Ua]bUh]cb dfcWYXi fYg/
- qdYWJU``Wcbq]XYfUHjcb`]b`H\Y`Yj YbhcZ]``bYgg`cf`a]gUXj Ybh fY/
- gh XYbhYei]miUbX'X]qUV]`]m/
- UbX'ch\Yf'YggYbhJU`'UWUXYa]W]bZcfa UhJcbz'gYY

\hdg.#k k k "Ufhg"i bgk "YXi "Ui #W ffYbhgh XYbhg#UWJXYa]W]bZcfa Uh]cb#dfchcWc`g![i]XY`]bYg#

.

⇒a U[Y'7fYX]h

D\chc'Vm'K_l'qcb'J_lhcflbc'Zfca 'DYI Y'q

7F = 7CG

7F = CG'Dfcj]XYf'7cXY.\$\$\$-,;

5W_bck `YX[Ya YbhcZ7ci bhfm

 $K Y : UW\underline{b} ck `YX[Y : h, Y : 6YXY[U : dY cd `Y : k \ c : UfY : h, Y : hfUX]h\underline{b} cb : `W ghc X]Ubg : c Z : h, Y ``UbXg : cb : k \]WX : I B G K ? Ybg]b[hcb : WUa di g :]g ``c WUhY X''$