

# **MDIA3006**

DfcXi Wgcb Gh X]c

Gi a a Yf''##'&\$%-

## 7ci fgY'Cj Yfj ]Yk

## Ghuzz 7 cbhuWh8 Yhu]`g

#### '7cbj Ybcfg'

B Ua Y	9a U]`	5j U]`UV]`] <b>m</b>	@cWJhjcb	D\cbY
5`mggU'F ch\k Y``	Ü	,	KYVghYf 6i]`X]b[ '' ‱	\$& -',)*,\$+

#### GWkcc~7cbhJWh~abZcfa Uh]cb

Fcca " &ž`Yj Y`" FcVYfhK YVghYf`6i ]`X]b[

D\cbY.'f\$&E'-',)'(,)\*

9a U]` gUa 4 i bgk "YXi "Ui

K YVg]hY. \hdg.#gUa "Ufhg"i bgk "YXi "Ui

 $\label{eq:hamiltonian} $$HY'GWKcc``cZhY'5ftg'UbX'AYX]U'kci`X``]_Y'tc'FYgdYWM\cong \cong m5W_bck`YX[Y'h\Y'HfUX]tjcbU``7i gtcX]Ubg\cong h\Y'6YXY[U'`fPYbg]b[tcb'WJa di g\cong tz'; UX][U'`fP]tmUbX'5fth/ '8Yg][b'7Ua di gYg\cong tubX't\Y'B[i bbUk U` dYcd'Y'fbi gtfU']Ub'8YZYbW': cf\w'5\\WXYa m']b'7UbVYffU\cozh\Y'`UbXg'k\YfY'YUW\cozh\Y'YUW\cozh\Y''UbXg'k\YfY'YUW\cozh\Y'' \cozh\Y''\UbXg'k\YfY'YUW\cozh\Y'' \cozh\Y''\UbXg'k\YfY'YUW\cozh\Y'' \cozh\Y''' \cozh\Y''' \cozh\Y''' \cozh\Y''' \cozh\Y''' \cozh\Y''' \cozh\Y''' \cozh\Y''' \cozh\Y''' \cozh\Y'''\UbXg'k\YfY'YUW\cozh\Y''' \cozh\Y''' \cozh\Y'''' \cozh\Y''' \cozh\Y'''' \cozh\Y''' \cozh\Y'''' \cozh\Y''' \cozh\Y'''' \cozh\Y''' \cozh\Y''' \cozh\Y''' \cozh\Y'' \cozh\Y''' \cozh\Y''$ 

## 7ci fgY 8YW] g

7 fYX]hDc]bhg\*\*

## Gi a a UfmcZh\Y 7ci fgY

Gi VYWh5fYU. A YX]U

\$\delta DfcXi Who Ghi X]c mci k \\ \delta k \\ \delta \delta \\ \delta \

## 7 ci fqY @YUfb]b[ Ci hMca Yq

- % 8 Ya cbglfUhY 'g\_]```]b`dfcZYgg]cbU``dfUWf]WYž'cf[ Ub]gUh]cbž'h]a Y`a UbU[ Ya Ybhž'Wca a i b]WUh]cb`'UbX'U dYfgcbU``dfcXi Wf]cb`glm`Y
- &" F YqdcbX'hc'Wf|h|WU`ZYYXVUW\_']b'U'dfcZYqq]cbU`UbX'WfYUh|j Y'k Um'
- ' "8Ya cbghfuhY`Ub`i bXYfghUbX]b[`cZh\Y`fY`Uh]cbg\]d`cZZcfa žWcbhYbhUbX`Ui X]YbWY`]b`U`a YX]U dfcXi Whcb"
- ("5fh]W'`UhY`h\Y]f'd`UWY`]b'h\Y'k]XYf'AYX]U']bXi ghfm

## HYUWX]b[ GhfUhY[]Yg

DfcXi Wfjcb`Ghi X]c`]g`XYg][ bYX`hc`fYUXmmci `Zcf`Z hi fY`Ya d`cma Ybhi]b`h\Y`a YX]U`dfcXi Wfjcb`]bXi ghfm'``5 dfcZygg]cbU``dfcXi Wfjcb`ghi X]c`Ybj ]fcba Ybhik ]```VY`WfYUhYX`k ]h\]b`Wci fgY`fcca g"

Mci 'k ]``VY'gi ddcfffYX'hc'k cf\_'cb'U'gdYW]ZJWdfcZYgg]cbU`'dfc'YWfidfcj ]XYX'Vm'U'W]Ybh''7`UggYg'k ]``VY qffi Wfi fYX'hc'qi ddcffmci f'dfcXi Wficb'a Yf\cXg'UggcW]UfYX'k ]h\mci f'gY`YWfX'W]Ybh'Vf]YZ'

Mci 'k ]```\Uj Y'cddcfh b]h]Yg'hc.
!a YYhk ]h\ 'h\ Y'W]Ybhg'UbX'X]gWi gg'h\ Y'Vf]YZ#g"
!Yb[ U[ Y']b'UWnjj ]h]Yg'hc'dfca chY'WfYUhjj Y'UbX'hYW\b]WU``g\_]```XYj Y`cda Ybh'
!VYWca Y']a a YfgYX'']b'dfUWnjWU`'dfcXi Wnjcb'fYgYUfW\"
!k cf\_'Wc``UVcfUhjj Y`mfbf']b'hYUa g'k \YfY'bYWYggUfm\"
!fYWY]j Y'Wf]h]WU`'ZYYXVUW\_'UbX'gi ddcfh'Zfca 'h\ Y'`YWni fYfz'dYYfg'UbX'h\ Y'W]Ybh'
!d]hW\'Ub']XYU'UbX'dfYdUfY'U'dfcYWnidfcdcgU`']b'fYgdcbgY'hc'h\ Y'7`]Ybh'Vf]YZ'

Mci 'k ]```VY 'YbWci fU[ YX 'hc 'hJ\_Y 'fYgdcbg]V]`]mmZcf'mci f'dfcZYgg]cbU``dfUWf)W' Vm !dfYdUf]b[ 'U'dfcZYgg]cbU``dfcdcgU``]bWi X]b[ 'U'dfcXi Wf]cb 'gWXYXi 'Y'UbX'Vi X[ Yh' !cf[ Ub]g]b[ 'a YYh]b[ g'k ]h\ 'mci f'W]Ybh' !Vcc\_]b[ 'dfcXi Wf]cb 'gdUWfg'UbX'Yei ]da Ybh' !XYj Y`cd]b[ 'UbX'[ Uh\Yf]b[ 'U``'h\Y'fYgci fWfg'mci 'fYei ]fY 'hc '[ Yh'h\Y'cV'XcbY" !dUfh]\M]dUh]b[ ']b 'fY[i `Uf]bZcfa U``ZYYXVUW\_gYgg]cb"

D`YUgY`fYZYf`hc`h\Y`a X]U'	\$\$* DfcXi	Whjcb Gh X]c A	CCX.X.K	YVg]hY	Zcf'U``i	d.pc.;	XUHY.	]bZcfa	Uh]cb'	UbX
UggYgga YbhXYhJ]`g"										

#### 5 hmy b X Ub WY F Yei ] f Ya Yb hg

H\]g`]g`Ub`]bhYbg]j Y`dfUWfJWU``dfcXi Wf]cb`Wci fgY`UbX`]h]g`YggYbhJU``h\Uh'ghi XYbhg`UhhYbX`U```h]a YhUv`YX WUgg`gYgg]cb`UbX`UggcWJUhYX`dfcXi Wf]cb`a YYh]b[ g"`5`ghi XYbh]g`YI dYWhYX`hc`UhhYbX`U```ZUWY!hc!ZUWY WcbhUWi\ci fg"

₹Uʻghi XYbhYl dYf]YbWrgʻ]``bYggža ]gUXj Ybhi fYʻcfʻch\YfʻcWW ffYbWrʻh\Uha U\_YgʻUVgYbWʻZfca ʻU WUgg#UWfj ]hmi bUj c]XUV`YžcfʻYl dYWgʻhcʻVYʻUVgYbhZfca ʻUʻZcfh\Wda ]b[ˈWUgg#UWfj ]hmžh\Ymg\ci `XʻgYY\_ dYfa ]gg]cbʻZfca ʻh\Yʻ7 ci fgYʻ5i h\cf]hmžʻUbXʻk \YfYʻUdd`]WUV`Yžh\Y]fʻfYei Yghg\ci `XʻVYʻUWWda dUb]YXʻVmUb cf][]bUʻʻcfʻWrfh]ZJYX`WdmcZUʻa YX]WU``WYfh]ZJWUhYʻcfʻch\YfʻZcfa ʻcZUddfcdf]UhYʻYj ]XYbWY''

 $\label{thm:condition} $$HY'a ]b]a i a `Ulfn'bXUbW'fYei ]fYa YbfiZcf'f\]g'Wci fgY']g', $i `gi ddcffn'X'VmXcW a YbfUf]cb'Yl d`U]b]b[UVqW'bW'g''$ 

## 7ci fgY'GWXYXi `Y

#### J]Yk 'WUgg'ha YHUV'Y

#### H]a YHJV`Y

8UHY	Hmd Y	7 cbhYbh
K YY_"%"&">Ubi Ufm!"* >Ubi Ufm		
K YY_^&^+^>Ubi Ufm!^% >Ubi Ufm		
K YY_" ."%( ">Ubi Ufm!"&\$ >Ubi Ufm		
K YY_^(.^&%'>Ubi Ufm!^&( : YVfi Ufm		

## FYgci fWyg

## DfYgWf]VYX F Ygci fWYg

5 [ccX'ei U`]mi\UfXXf]j Y Zcf'dfc YWik cf\_'UbX'cb[c]b[ 'VUW\_!i dg'cZdfc YWg"

## FYWca a YbXYX FYgci fW/g

7 fYUh]b[ 'Mci f'8][ ]hU`Dcfh2c`]c. 'H\Y'9ggYbh]U`'; i ]XY'hc'G\ck WUg]b[ 'Mci f'8Yg][ b'K cf\_'Cb`]bY"

FYZYfihoih\Yia X]U' \$\$\* DfcXi WhjobiGhi X]o A ccXiYik YVg]hYiZofii dihoiXUhYifYgciifWig"

## 7 ci fgY 9j U'i Uhjcb UbX 8 Yj Y'cda Ybh

## Gi Va ]gg]cb cZ5ggYgga YbhHUg\_g

#### Hi fb]h]b Gi Va ]gg]cb

Image: Ybwb: bh/f'u'dfcV'Ya k \Yb'Uhlya dhjb['hc'gi Va ]hmci f'Ugg][ ba Ybhh\fci [\'Hi fb]h]bž'd'YUgY

HY'Yd\cbY'9| h/fbu''Gi ddcfhcb'-', ) '' ' ' %cf'Ya U]''h\Ya 'cb'<u>Yl h/fbu'h/hgi ddcfh4 i bgk "YXi "Ui"</u> "'Gi ddcfh
\ci fg'UfY', .\$\$Ua '-'\\$\$.\$\$da 'cb'k YY\_XUmg'UbX'-.\$\$Ua '-').\$\$da 'cb'k YY\_YbXg'fl \*) 'XUmg'U'mYUfŁ" Image:

UfY'i bUV'Y'hc'gi Va ]hmci f'Ugg][ ba YbhXi Y'hc'U'ZJi 'hk ]h\'Hi fb]h]b'mci 'a UmUdd'mZcf'Ub'Yl h/bg]cbž'Vi hmci
a i ghfYhJ]b'mci f'h]\W\_Yhbi a VYf'Zfca '9| h/fbU''Gi ddcfhfU'cb['k]h\'Ubmch\Yf'fY'Yj UbhXcW a YbhgŁ'hc
]bWi XY'Ug'Yj ]XYbW' 'hc'gi ddcfhmci f'Yl h/bg]cb'Udd']\WJh]cb"'Imai 'Ya U]''9| h/fbU''Gi ddcfhmci 'k ]''

Ui hca Uh]\WJ''mfYW']j Y'U'h]\W\_Yhbi a VYfž'Vi h]Zmci 'hY'Yd\cbY'mci 'k ]'''bYYX'hc'gdYW]Z]\WJ''mUg\_'Zcf'cbY''

Hi fb]h]b'U'gc'dfcj ]XYg'i dXUhYg'cb'h\Y]f'gmghYa 'ghUh' g'cb'Hk ]hYf''

; YbYfU``mž'UggYgga YbhitUg\_g'a i ghVY'gi Va ]hhYX'Y`YWfcb]WU``mj ]U'Y]h\Yf'Hi fb]h]b'cf'U'A ccX`Y Ugg][ ba Ybh'' =b']bghUbWfg'k \YfY'h\]g']g'bchdcgg]V`Yž']hk ]```VY'ghUhYX'cb'mci f'Wci fgY'g'A ccX`Y'g]hY'k ]h\U`hYfbUh]j Y'gi Va ]gg]cb'XYhU]`g''

: cf]bZcfa Uh]cbcb`\ck 'hcgi Va ]hUgg][ ba Ybhgcb`]bY'j ]U'A ccX`Y.

#### \hdg.#gh XYbh'i bgk "YXi "Ui #\ck!gi Va ]hUgg][ ba Ybha ccX`Y

#### @UhY 5ggYgga YbhDYbU`h]Yg

Ghi XYbhgʻUfYʻfYgdcbg]V`YʻZcfʻh\Yʻgi Va ]gg]cbʻcZUggYgga Ybhilug\_gʻVmh\YʻfYei ]fYX`XUhYgʻUbXʻhJa Ygʻ' 8YdYbX]b[ˈcZh\Y`YI hYbhcZXY`Um]bʻh\Yʻgi Va ]gg]cbʻcZUbʻUggYgga Ybhilug\_ʻdUghih\YʻXi YʻXUhYʻUbXʻhJa Yž cbYʻcZh\YʻZc``ck ]b[ʻ`UhYʻdYbUʻhJYgʻk ]```Udd`mi b`YggʻgdYVJU`'Wcbg]XYfUhJcbʻcfʻUʻV`Ub\_YhYI hYbg]cbʻXi YʻhcʻU hYV\\b]WU``ci hU[Yʻ]gʻ[fUbhYX'': cfʻh\Yʻdi fdcgYʻcZ`UhYʻdYbUʻhm\WJ`W``UhJcbž'UʻʻXUmi']gʻXYYa YXʻhcʻVYʻYUV\\&(!\ci fʻdYf]cX`fcf`dUfhh\YfYcZcdUghh\YʻghJdi `UhYX`XYUX`]bYʻZcf`gi Va ]gg]cb''

K cf\_'gi Va ]hh/X ``Ygg'h\ Ub '%\$ `XUmg'UZh/f'h\ Y'gh]di `Uh/X `XYUX`]bY']g'gi V'YWhrc'U'XYXi Whjcb'cZ)ı 'cZh\ Y hch''Uk UfXUV`Y'a Uf\_'Zfca 'h\ Y'a Uf\_'h\ Uhk ci `X`\ Uj Y'VYYb'UW\]Yj YX']Zbch'Zcf'h\ Y'dYbU'mmZcf'Yj YfmXUm dUghh\ Y'gh]di `UhYX`XYUX`]bY'Zcf'gi Va ]gg]cb"'H\ Uh']gž'U'ghi XYbhk \c'gi Va ]hg'Ub''Ugg][ ba Ybhk ]h\ 'U gh]di `UhYX`XYUX`]bY'cZ(.\$\$da 'cb'%' A Um&\$%\* 'Uh'(.%\$da 'cb'%('A Um&\$%\* 'k ]``]bW f'UXYXi Whjcb'cZ%\$!"

#### HUg\_'k]h\'U'bcb dYfWfbhU[Y'a Uf\_

"-Zh\Y'hUg\_']g'a Uf\_YX'ci hcZ&) žh\Yb'`UhY'gi Va ]gg]cb'k]```UhhfUWiU'dYbU`hmcZU'XYXi Wf]cb'cZ%"&) 'Zfca 'h\Y a Uf\_'Uk UfXYX'hc'h\Y'ghi XYbhZcf'Yj Yfm&(!\ci f'dYf]cX'fcf'dUfhh\YfYcZcdUghh\Y'gh]di `UhYX'XYUX`]bY" 91 Ua d'Y. '5 'ghi XYbhgi Va ]hg'Ub'YggUm(, '\ci fg'UbX'%\$'a ]bi hYg'UZhYf'h\Y'gh]di `UhYX'XYUX`]bY"'H\Y'hchU` dcgg]V'Y'a Uf\_'Zcf'h\Y'YggUm']g'&) "'H\Y'YggUmfYWY]j Yg'U'a Uf\_'cZ%+"'H\Y'ghi XYbhg'a Uf\_']g'h\YfYZcfY'%+'- &) 'f\$"\$) 'I'' LQ1'% "&)

#### HUg k ]h\ U dYfWYbhU[ Y a Uf

₹ħ\Y`HJg\_`]gʻa Uf\_YXʻci hcZ%\$\$i ž'h\Yb``UhYʻgi Va ]gg]cbʻk ]```UhffUWhUʻdYbU`hmcZUʻXYXi WijcbʻcZ) i 'Zfca h\Y`a Uf\_'Uk UfXYX`hc`h\Y`ghi XYbhZcfYj Yfm&(!\ci fʻdYf]cX`fbfdUfhh\YfYcZddghh\Y`gh]di `UhYX`XYUX`]bY" 9I Ua d`Y. '5 ʻghi XYbhgi Va ]hgʻUbʻYggUm(, '\ci fgʻUbX`%\$`a ]bi hYgʻUZhYfʻh\Y`gh]di `UhYX`XYUX`]bY"`H\Y`YggUm ]gʻa Uf\_YX`ci hcZ%\$\i "'H\Y`YggUmfYWY]j YgʻUʻa Uf\_cZ\*, "'H\Y`ghi XYbhgʻa Uf\_`]gʻh\YfYZcfY`\*, '-'%) '1`)'

K cf\_'gi Va ]hhYX'%\$'hc'% 'XUmg'UZhYf'h\Y'gh]di `UhYX'XYUX`]bY'k ]``'VY'UggYggYX'UbX'ZYYXVUW\_'dfcj ]XYX Vi hU'a Uf\_'cZnYfc'k ]``'VY'fYWcfXYX'''=Zh\Y'k cf\_'k ci `X`\Uj Y'fYWY]j YX'U'dUgg'a Uf\_'Vi hZcf'h\Y'`UhYbYgg'UbX h\Y`k cf\_`]g`U`Wca di `gcfm'Wci fgY`Wca dcbYbhf\i fX`Y`fYei ]fYa Ybhz`U`gh XYbhk ]```VY`XYYa YX`hc`\Uj Y`a Yhh\UhfYei ]fYa Ybh/

K cf\_'gi Va ]hhYX`&\$`cf`a cfY`XUmg`UZhYf`h\Y`gh]di `UhYX`XYUX`]bY`k ]``bchVY`UWWdhYX`Zcf`UggYgga YbhUbX`k ]``fYWY]j Y`bc`ZYYXVUW\_ža Uf\_'cf`[ fUXY''=Zh\Y`UggYgga YbhHUg\_']g`U`Wca di `gcfmWca dcbYbhcZh\Y Wci fgY`U`ghi XYbhk ]``fYWY]j Y`Ub`l bgUh]gZJWcfm: U]``fl : L`[ fUXY`Ug`U`fYgi `hcZi bgUh]gZJWcfmdYfZcfa UbWY]b`Ub`YggYbh]U``Wca dcbYbhcZh\Y`Wci fgY"

 $H\ [g']bZcfa\ Uh]cb']g'U\ gc'Uj\ U]\ UV\ Y'Uh'\ \underline{hdg.\#k\ k\ k''Ufhg''i\ bgk''YXi'''Ui\ \#W\ ffYbHghi\ XYbhg\#UWUXYa\ ]W} ]bZcfa\ Uh]cb\#dfchcWc\ g!\ [i\ ]XY\ ]bYg\#$ 

#### Gi dd`Ya YbhUfm'UggYgga Ybhg`

H\Y`Zcfa `cZh\Y`gi dd`Ya YbhUfmUggYgga YbhbYYX`bchVY`]XYbh]\WU``hc`h\Y`cf][ ]bU``UggYgga YbhVi h`]ha i gh UggYgg`h\Y`gUa Y``YUfb]b[ `ci h\can Yg"

5 'gi dd`Ya YbhUfm'UggYgga Ybhik]``'VY'cZYfYX'hc'U'ghi XYbhik \c'ZU]`g'Ub'UggYgga YbhihUg\_']b'Y]h\Yf'cZh\YZc``ck]b['W]fW a ghUbWfg.

- 'Gi dd'Ya YblUfmUggYgga Ybhk ]```VY cZYfYX'hc 'Ubmgh XYbhk \c 'ZJ]'g'Ub 'UggYgga YbhlUg\_']Zh\Y]f'fYei Ygh Zcf'GdYWJU`'7 cbg]XYfUhJcb 'Zcf'h\UhilUg\_']g'Uddfcj YX"'H\Y'a Uf\_'Uk UfXYX 'Zcf'h\Y'UggYgga YbhlUg\_'k ]```VY VUgYX'qc'Y`mcb'h\Y'gi dd'Ya YbhUfmUggYgga Ybh'
- 'K \YfY'U'ghi XYbh'ZJ]`g'Ub'UggYgga Ybh'HJg\_']b'U'Wci fgY']b'h\Y'Z]bU`hYfa 'cZh\Y]f'dfc[fUa ž'Vi hXcYg'bch \Uj Y'Ub'Uddfcj YX'GdYW]U`'7 cbg]XYfUh]cb'Zcf'h\Uh'HJg\_žgi dd`Ya Ybh'Jfm'UggYgga Ybh'k]``'gh]```VY'cZYfYX']b WJgYg'k \YfY'dUgg]b['h\Y'HJg\_'k ci `X'\Uj Y'fYgi `h\X']b'h\Y'ghi XYbh'dUgg]b['h\Y'Wci fgY'UbX'Wca d`Yh]b['h\Y dfc[fUa "

GWkcc`gʻa UmWkccgYʻhcʻcZZYfʻgi dd`Ya YbhUfmUggYgga Ybhgʻi bXYfʻch\YfʻVJfW a ghUbWrgʻh\Ubʻh\cgYʻ`]ghYX UVcj Y"8YWJg]cbgʻVmGWkcc`gʻhcʻcZZYfʻgi dd`Ya YbhUfmUggYgga Ybhgʻi bXYfʻch\YfʻVJfW a ghUbWrgʻh\Ubʻh\cgY`]ghYX`UVcj Y`g\ci `X`VY`[i]XYX`Vm`cWUʻdfcWrggYgʻhc'dfca chY'df]bWJd`YX`UbX`Wcbg]ghYbhXYWJg]cb!a U\_]b["

H\Y`a Uf\_`Uk UfXYX`Zcf`U`gi dd`Ya YbHUfmiUggYgga Ybhž`]b`h\Y`UVgYbWI`cZGdYWJU``7 cbg]XYfUh]cbž`k ]```VY WUddYX.

- K \YfY`U`gi dd`Ya YbhUfmUggYgga Ybh`]g`dfcj ]XYX`Zcf`U`gh XYbhk\c`ZJ]`g`Ub`UggYgga Ybh'HJg\_`]b`Ubm Wti fgYž'h\Y`ZbU``a Uf\_`Uk UfXYX`Zcf`h\Y`UggYgga Ybh'HJg\_`k]``VY`WUddYX`Uh)\\$i "
- •K \YfY'U'gi dd`Ya YbhUfm'UggYgga Ybh']g'dfcj ]XYX'hc'U'gh XYbh'k ]h\'U': U]''VUgYX'cb'h\Y'cj YfU`''Wci fgY fYgi `hž'h\Y'Z]bU``a Uf\_'Zcf'h\Y'Wci fgY'k ]`''VY'WUddYX'Uh) \$\| \| \|

 $H\setminus ]g']bZcfaUh]cb']g'U`gc'UjU]`UV`Y'Uh$ 

\hdg.#k k k "Uffg"i bgk "YXi "Ui #W ffYbhgh XYbhg#UWJXYa ]W]bZcfa Uhcb#dfchcWc`g![i ]XY`]bYg#

#### GdYW/U`7cbg]XYfUh|cb5dd`|WUh|cbg

Mci 'WUb'Udd`m'Zcf'gdYWJU``Wcbg]XYfUhJcb'k \Yb']``bYgg'cf'ch\Yf'WJfW a ghUbWrg']bhYfZYfY'k ]h\ 'mci f UggYgga Ybh'dYfZcfa UbWr"

 $G ] \underline{W}_b Y g g \check{z} \check{a} ] \underline{g} U X \underline{j} Y b h \underline{f} Y \dot{c} \underline{f} \dot{c} h \underline{Y} \underline{f} \dot{W} \underline{f} W \underline{a} \underline{g} \underline{f} U b W \underline{f} \underline{g} \dot{v} \underline{Y} \underline{m} \underline{c} \underline{b} \underline{X} \dot{m} \underline{c} \underline{i} \underline{f} \dot{w} \underline{c} \underline{b} \underline{f} \underline{c} \dot{a} \underline{u} \underline{m}$ 

ł DfYj Ybhmci Zfca Wca d`Yhjb[ 'U'Wci fgY'fYei ]fYa Ybhž

ł? YYd mci Zfca 'UlthybX]b[ 'Ub 'UggYggUV'Y 'UWt]j ]tmž

ł Ghod moi igi Va ]hh]b[ 'UggYggUV'Y'k cf\_'Zcf'U'Wci fgYž

 $\label{eq:continuity} $$ f'G][b]ZWbhmUZYWhmci f'dYfZcfa UbWf']b'UggYggUV'Y'k cf_ž'VY']hU'Zcfa U`'YbX!cZhYfa 'Yl Ua ]bUh]cbž'U WUgg'hYghz'U'`UVcfUhcfmhYghz'U'gYa ]bUf'dfYgYbhUh]cb'cf'Ubmch\Yf'Zcfa 'cZUggYgga Ybh'$ 

: cf Z fh\Yf`XYHJ]`g`]b`fY`Uhjcb`hc`GdY\JU``7 cbg]XYfUhjcb`]b\W X]b[ `"K \Yb`hc`5dd`m'`Z'"< ck 'hc`5dd`m'`UbX "Gi ddcfhjb[ '8 c\W a YbHJhjcb"'d`YUgY`fYZYf`hc`h\Y`GdY\JU``7 cbg]XYfUhjcb`k YVg]hY.`\hhdg.#gh`XYbh'i bgk "YXi "Ui #gdY\JU`!\Wcbg]XYfUhjcb

.

## 5 WUXYa ]W<cbYghmUbX D`U[ ]Uf]ga

D`U[]Uf]ga `]g`i g]b[ 'h\Y`k cfXg`cf`]XYUg`cZch\Yfg`UbX`dfYgYbh]b[ 'h\Ya `Ug`mci f`ck b"'\lefi\Wb'hU\_Y`a Ubm Zcfa gžZfca `XY`]VYfUhY`W\YUh]b[ 'hc`UVW]XYbhU`mWcdm]b[ 'Zfca `U`gci fW'k ]h\ci hUW\_bck `YX[ Ya Ybh'

IBGK [fcidgdu[]uf]ga ]bhch\YZc``ck]b[ WuhY[cf]Yg.

7 cdm]b[.'i g]b['h\Y'gUa Y'cf'j Yfmg]a]`Uf'k cfXg'hc'h\Y'cf][]bU`hYl h'cf']XYU'k]h\ci h'UW\_bck `YX[]b['h\Y gci fW'cf'i g]b['ei chUh]cb'a Uf\_g"'H\]g'U`gc'Udd`]Yg'hc']a U[Ygž'Ufh'UbX'XYg][b'dfcYWgž'Ug'k Y``'Ug dfYgYbhUh]cbg'k \YfY'gca YcbY'dfYgYbhg'Ubch\Yf'g']XYUg'cf'k cfXg'k]h\ci h'WfYX]h'

=\uddfcdf]UhY 'dUfUd\fUg]b[ .'7\Ub[ ]b[ 'U'ZYk 'k cfXg'UbX'd\fUgYg'k \]'Y 'a cghmfYhJ]b]b[ 'h\Y'cf][ ]bU`
ghfi Whi fY 'UbX#cf'dfc[ fYgg]cb'cZ]XYUg'cZh\Y'cf][ ]bU`ž'UbX']bZcfa Uh]cb'k ]h\ci h\UW\_bck `YX[ Ya Ybh''H\]g'U`gc
Udd`]Yg']b'dfYgYbhUh]cbg'k \YfY 'gca YcbY'dUfUd\fUgYg'Ubch\Yf'g']XYUg'cf'k cfXg'k ]h\ci h\UhYX]hUbX'hc
d]YW]b[ 'hc[ Yh\Yf'ei chYg'UbX'dUfUd\fUgYg']bhc'U'bYk 'k \c`Yž'k ]h\ci h\Uddfcdf]UhY'fYZYfYbW]b[ "

7 c``i g]cb.'k cf\_jb['k]h\ch\Yfg'Vi hdUgg]b['cZZh\Y'k cf\_'Ug'U'dYfgcb'g']bX]j ]Xi U``k cf\_"'7 c``i g]cb'U`gc ]bWi XYg'dfcj ]X]b['mci f'k cf\_'hc'Ubch\Yf'ghi XYbhVYZcfY'h\Y'Xi Y'XUhYžcf'Zcf'h\Y'di fdcgY'cZh\Ya d`U[]Uf]g]b['UhiUbmh]a Yž'dUm]b['Ubch\Yf'dYfgcb'hc'dYfZcfa 'Ub'UWUXYa ]WhUg\_ž'ghYU']b['cf'UWei]f]b[ Ubch\Yf'dYfgcb'g'UWUXYa ]Wk cf\_'UbX'Wcdm]b[']hz'cZYf]b['hc'Wca d'YhY'Ubch\Yf'dYfgcb'g'k cf\_'cf'gYY\_]b[ dUma YbhZcf'Wca d'Yh]b['UWUXYa ]Wk cf\_"

±bUddfcdf]UhY`W]hUh]cb.`7]h]b[`gcifWrg`k\]W\`\UjY`bchVYYb`fYUXžk]h\cihUW\_bck`YX[]b[`h\Y`´gYWcbXUfm´gcifWrZfca`k\]W\`\_bck`YX[Y`cZh\Ya`\Ug`VYYb`cVhU]bYX"

8 i d`]\W\n]cb`ffgY`Z\d`U[]\Uf]ga "Ł`gi Va]\n]b[`mci f`ck b`k cf\_z`]b`k \c`Y`cf`]b`dUffz`k \YfY`]h\Ug`dfYj]ci g`m VYYb`dfYdUfYX`cf`gi Va]\nYX`Zcf`Ubch\Yf`UggYgga Ybhcf`\\cf\\text{i fgY`UhI\_BGK\_`cf`Ubch\Yf`i b]j Yfg]\m'

7 cffYWnfYZYfYbWlb[ 'dfUWnWyg.

- DUfUd\fUg]b[žgi a a Uf]g]b[žYggUmk f]h]b[ 'UbX h]a Y a UbU[Ya Ybh
- 5ddfcdf]UhY'i gY'cZUbX'Uhtf]Vi h]cb'Zcf'U'fUb[Y'cZa UhYf]U`g']bWi X]b['hYl hž']a U[Ygž'Zcfa i `UY'UbX WbWYdhg"

±0X]j ]Xi U``Ugg]ghUbWr`]g`Uj U]`UV`Y`cb`fYei YghZfca `H\Y`@YUfb]b[ `7 YbhY`f\hd.#k k k "`Wi bgk "YXi "Ui #£" Gh XYbhg`UfY`U`gc`fYa ]bXYX`h\UhWUfYZ ``hja Y`a UbU[ Ya Ybh]g`Ub`]a dcfhUbhdUfhcZgh XmUbX`cbY`cZh\Y ]XYbh]Z]YX`WUi gYg`cZd`U[ ]Uf]ga `]g`dccf`hja Y`a UbU[ Ya Ybh'`Gh XYbhg`g\ci `X`U``ck `gi Z]W]Ybh'hja Y`Zcf fYgYUfW\žXfUZh]b[ `UbX`dfcdYf`fYZYfYbW]b[ `cZgci fWfg`]b`dfYdUf]b[ `U``UggYgga Ybh']hYa g"

IBGK @]VfUfmU`gc`\Ugʻh\Y`9@G9`hcc``UjU]`UV`Y`hc`Ugg]ghmci`k]h\`mcif`ghiXmUhIBGK "'9@G9`]gXYg][bYX`hc`]bhfcXiVW`bYk`ghiXYbhg`hc`ghiXm]b[`UhIBGK`Vih]hWUb`U`gc`VY`U`[fYUhfYZfYg\Yf`Xif]b[`mcifqhiXm"

7 ca d'Yhlb[ 'h\Y'9@&9'hi hcf]U`'UbX'ei ]n'k ]`'YbUV'Y'mci 'hc.

 UbU`mgY`hcd]\Mgž'd`Ub`fYgdcbgYg`UbX`cf[Ub]gY`fYgYUf\W\`Zcf'U\WXYa]\Wk f]hjb[`UbX`ch\Yf UggYgga YbhiHUg\_g

- i bXYfgfUbX mci f'f][\hg'UbX'fYgdcbg]V]`]hJYg'Ug'U'gh XYbhUhl BGK
- VY`Uk UfY`cZd`U[]Uf]ga ž`Wcdmf][\hz'l BGK `Gh XYbh7cXY`cZ7cbXi WhUbX`5VWWdhUV`Y`l gY`cZ I BGK `=\forall H`F Ygci f\W\g`Dc`]\m\m
- VY 'Uk UfY 'cZh\Y 'ghUbXUfXg 'cZVY\Uj ]ci f'Yl dYWYX 'cZYj YfmcbY ']b 'h\Y 'l BGK 'Wca a i b]hm
- `cWUHY 'gYfj ]WYg'UbX ']bZcfa UH]cb'UVci hI BGK 'UbX'I BGK '@]VfUfm

Gca Y'cZh\YgY'UfYUg'k]``VY'ZJa]`]Uf'hc'mci žch\Yfg'k]``VY'bYk"'; U]b]b['U'gc`]X'i bXYfgHJbX]b['cZU``h\YfY`UhYX'UgdYWhg'cZ9@&9'k]``\Y`d'mci 'a U\_Y'h\Y'a cghicZmci f'ghi X]Yg'Uh'l BGK "'\\hd.##gi V'YWfi |XYg"`]VfUfm'i bgk "YXi "Ui #\`]qY#JVci hY`]qY